# Alabama Reading and Mathematics Test 

## Item Specifications

for

## Mathematics

## Grade 6



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Montgomery, Alabama
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## NUMBER AND OPERATIONS

## Content Standard 1

Demonstrate computational fluency with addition, subtraction, multiplication, and division of decimals and fractions.

## Item Type

Multiple-choice
Gridded

## Additional Information

Mixed numbers may be used.
Common and uncommon denominators may be used.
Fractions may be in simplest form.
No word problems/context problems will be used.
No calculators may be used.
One of the options may be NH, which means "Not Here."

## Sample Multiple-Choice Items



## ARMT GRADE 6 MATHEMATICS



A $\frac{120}{7}$
C $\frac{1}{2}$
B $\frac{42}{5} *$
D $\frac{2}{7}$
6. $3.12 \div 0.6=\square$
A 3.76
C 1.872
B 2.52
D $5.2^{*}$



## ARMT GRADE 6 MATHEMATICS

## Answer Key

## Content Standard 1

## Sample Multiple-Choice

1. C
2. C
3. D
4. A
5. B
6. D
7. B
8. A
9. B

## NUMBER AND OPERATIONS

## Content Standard 2

Solve problems involving decimals, percents, fractions, and proportions.

## Item Type

Multiple-choice
Gridded
Open-ended

## Additional Information

Multi-step problems with decimals and/or percents may be used.
Determining discount, sale price, or original price may be required.
Determining amount of interest may be required.
Tables and charts may be used.
Pictures may be used.
Word problems may be used.
Fractions in their simplest form may be required.
Estimation may be required.
Determining the total payment for a loan may be required.
Determining ratio or proportion may be required.
Determining rate or time in a work problem may be required.
Determining the percent of change may be required.

## Sample Multiple-Choice Items

(continued on next page)

1. Mr. Miele had enough sugar to make $\frac{3}{4}$ of a batch of cookies. To make a whole batch, he needed $\frac{1}{3}$ cup of sugar.


How many cups of sugar did Mr. Miele have?

| $\frac{1}{4}$ | $\frac{5}{12}$ | $\frac{13}{12}$ | $\frac{2}{1}$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{A}^{*}$ | $\mathbf{B}$ | $\mathbf{C}$ | $\mathbf{D}$ |

2. 

Paper Goods Store

| Paperware |  |  |
| :--- | ---: | :---: |
| Plates | $\$ 2.99$ |  |
| Napkins | $\$ 3.69$ |  |
| Cups | $\$ 2.39$ |  |

Loraine bought 3 packages of plates and 5 packages of napkins for a party.

If the prices on the sign included tax, how much change should Loraine have received from $\$ 30$ ?

3. Which is the closest estimate for $\mathbf{3 3 \%}$ of 520 ?

| 52 | 170 | 180 | 487 |
| :---: | :---: | :---: | :---: |
| $\mathbf{A}$ | $\mathbf{B}^{*}$ | $\mathbf{C}$ | $\mathbf{D}$ |

4. Dana recorded the number of days her brother wore sneakers to school and the number of days he wore loafers to school. The ratio of the number of days he wore sneakers to school to the number of days he wore loafers to school was 5 to 2.

If Dana observed and recorded her brother's choice of shoes for 49 days, how many times did he wear sneakers?

2
A
B
C*
D
5. Keely has walked $1 \frac{1}{6}$ miles on her way from the Post Office to the Jordan Library. She still has to walk $1 \frac{5}{12}$ miles to reach the library.


How many miles in all did Keely have to walk from the Post Office to the Jordan Library?
A $\frac{1}{3}$ miles
C $2 \frac{1}{3}$ miles
B $\frac{1}{6}$ miles
D $2 \frac{7}{12}$ miles*

## ARMT GRADE 6 MATHEMATICS

## Sample Gridded Items

1. Anna went to the store to buy a new dress. The dress she chose was $30 \%$ off the original price.

What was the original price of the dress that was marked down $\$ 13.95$ ?

Mark your answer in the answer grid.
3. A digital camera originally cost $\$ \mathbf{5 9 . 9 5}$. Its cost decreased 15\%.

What is the sales price of the camera, not including tax?

Mark your answer in the answer grid.
2. There are $\mathbf{6 5 0}$ sixth-grade students in the city. Forty-six percent of the students are boys.

How many of the sixth-grade students in the city are boys?

Mark your answer in the answer grid.
4. The science department has a budget of $\mathbf{\$ 4 0 0}$ per year for supplies.

If the science teachers have spent $60 \%$ of the supply budget for the year, how much money is left for supplies?

Mark your answer in the answer grid.
5. Mr. Jennings spent $\mathbf{3 0 \%}$ of his gardening budget to purchase rose plants.

If he spent exactly $\$ 60$, including tax, on rose plants, how much money should he have left over?
6. The price of a shirt was reduced from \$32 to \$24 during a one-day sale. What is the percent of discount on the price of the shirt during the sale?

Mark your answer in the answer grid.
7. Ashley plans to run a total of 24 miles this week. If Ashley has already run $25 \%$ of the total distance, how many more miles does she plan to run this week?

Mark your answer in the answer grid.

Mark your answer in the answer grid.

## Sample Open-Ended Items

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.

1. The manager at Ashley's Dress Shop took $\mathbf{1 0 \%}$ off the price of all dresses. One month later, the manager took an additional $15 \%$ off the price of the same dresses.
a. What was the price of a $\mathbf{\$ 1 2 0}$ dress after the first price reduction?
b. What was the price of a $\mathbf{\$ 1 2 0}$ dress after the second price reduction?
c. Would the price be the same if the store manager simply took $\mathbf{2 5 \%}$ off the original price of all the dresses?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
2. Lauren and Thomas stuffed envelopes for an election campaign. Lauren stuffed 56 envelopes in 5 minutes and Thomas stuffed 42 envelopes in 3.5 minutes.
a. How many envelopes did Lauren stuff per hour?
b. How many envelopes did Thomas stuff per hour?
c. At the same rate of stuffing envelopes, about how long should it take Lauren and Thomas, working together, to stuff a total of 2604 envelopes?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
3. A food server at Harper's Restaurant is paid $\$ 5$ per hour plus a $15 \%$ tip on the money made on each table he serves.

A food captain at Bea's Fine Dining is paid $\$ 8$ per hour plus a $\mathbf{1 2} \%$ tip on the money made on each table he serves.
a. If the food server at Harper's Restaurant worked 25 hours and the total amount of money made at his tables was $\$ 4,000$, what was his total pay for the week?
b. If the food captain at Bea's Fine Dining worked 25 hours and the total amount of money made at his tables was $\$ 4,000$, what was his total pay for the week?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
4. Ally had a bag of $\mathbf{4 0}$ beads. The bag contained 30 red beads and 10 gold beads. After she gave Louise 21 red beads and some gold beads, Ally noticed that the ratio of red to gold beads was the same as it was before she gave any beads to Louise.
a. How many gold beads did Ally give to Louise?
b. How many red beads and gold beads did Ally have left?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
5. Georgie put $\$ 500$ in her savings account, earning interest at a rate of $\mathbf{4 \%}$ each year. She did not make any more deposits or withdrawals.
a. How much money was in the account after one year?
b. How much money was in the account after 4 years?
c. Was the amount of money earned in interest the same or different each year?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
6. The Smiths borrowed $\$ 1,500$ at $\mathbf{6 \%}$ simple annual interest to buy a used motorcycle. They paid it back in 12 equal monthly payments.
a. What was the total amount paid back?
b. What was the amount of each payment?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
7. A computer company expects to increase the number of people it employs at a rate of $\mathbf{4 \%}$ per year for the next four years.
a. If the computer company has 600 employees now, in how many years will it have over 650 employees?
b. If the computer company is able to increase the number of people it employs at a rate of $8 \%$ per year, when will it have over 650 employees?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
8. The tally chart below shows the gymnastics scores for $\mathbf{2 5}$ gymnasts at a competition.
Gymnastic Scores

| Score | Frequency |
| :---: | :---: |
| $0-5.9$ | II |
| $6.0-6.9$ | III |
| $7.0-7.9$ | HI III |
| $8.0-8.9$ | IHI II |
| $9.0-10.0$ | I\|II |

a. What percent of the scores were 7.0 or above?
b. If the blue ribbon score is a 9.0 or more, what percentage of gymnasts did not receive a blue ribbon?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
9. Bernie bought a computer for $\$ 900$. One year later, the value of the computer was $\mathbf{\$ 7 2 0}$.
a. How much did the value of the computer drop?
b. What is the percent of change in the value of the computer?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

# ARMT GRADE 6 MATHEMATICS 

## Answer Key

## Content Standard 2

Sample Multiple-Choice

1. A
2. A
3. B
4. C
5. D

## Sample Gridded

1. $\$ 46.50$
2. 299
3. $\$ 50.96$
4. $\$ 160$
5. $\$ 140$
6. $25 \%$
7.18

## ARMT GRADE 6 MATHEMATICS

## Sample Open-Ended

## 1. Sample Response(s):

a. $\$ 120 \times 0.10=\$ 12, \$ 120-\$ 12=\$ 108.00$

OR
I used my calculator to multiply 120 and $10 \%$ and this gave me a discount of $\$ 12.00$. I then subtracted $\$ 12$ from $\$ 120$. The price of the dress is $\$ 108.00$. OR
I multiplied 120 and $10 \%$. This equaled a discount of $\$ 12.00$. After that, I subtracted $\$ 12$ from the original dress price of $\$ 120$. The price of the dress is now \$108.00.
b. $\$ 108 \times 0.15=\$ 16.20, \$ 108-\$ 16.20=\$ 91.80$

OR
I used my calculator to multiply 108 and $15 \%$ and this gave me a discount of $\$ 16.20$. I then subtracted $\$ 16.20$ from $\$ 108$. The price of the dress after the second discount is $\$ 91.80$.

## OR

I first multiplied $\$ 108$ by $15 \%$ ( 0.15 ). This gave me an answer of $\$ 16.20$. Then, I subtracted $\$ 16.20$ from $\$ 108$. This gave me an answer of $\$ 91.80$. This is the price of the dress after the second discount.
c. No, the price would not be the same. If the manager took $25 \%$ off the original price of the dress, then the dress would be $\$ 90.00$ instead of $\$ 91.80$.
$(\$ 120 \times 0.25=\$ 30, \$ 120-30=\$ 90$.

## OR

I used my calculator to find that $25 \%$ off the original price would be $\$ 90.00$ instead of the $\$ 91.80$ that was found in part $\mathbf{b}$. No, the price would not be the same.

| Score Point | Response Attributes |
| :---: | :---: |
| 3 | All is correct. |
| 2 | All logics or explanations are correct. <br> OR <br> Two correct logics or explanations and correct answers for two problems or drawings. <br> OR <br> One correct logic or explanation and correct answers for all problems. |
| 1 | One or more answers to problems are correct. OR <br> One correct logic or explanation. |
| 0 | None is correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.) |

## ARMT GRADE 6 MATHEMATICS

## 2. Sample Response(s):

a. $\frac{60}{5}=12 ; 56 \times 12=672$ envelopes

OR
$\frac{56}{5}=\frac{x}{60}, 56 \times 60=5 \times x, 3360=5 x, 3360 \div 5=672$ envelopes

## OR

1 hour equals 60 minutes. There are 125 -minute intervals in 60 minutes.
I multiplied 56 times 12 to get 672 envelopes per hour.
b. $60 \div 3.5 \times 42=$ approximately 720 envelopes.

OR
I used my calculator to figure out how many times 3.5 goes into $60(60 \div 3.5)$.
I then took that answer and multiplied it times 42 to get approximately 720 envelopes per hour.

## OR

I found out how many times 3.5 goes into 60 by dividing the two numbers ( $60 \div 3.5$ ). Then, I took the answer and multiplied it times 42 . Thomas stuffed approximately 720 envelopes per hour.
c. $672+720=1392$
$2604 \div 1392=1.87$
Round up to 2. About 2 hours.
OR
About two hours. Take the answer from part a (672) and the answer from part b (720) and add these two together (1392). Then, take 2604 and divide it by 1392 . This gives an answer of 1.87 which rounds to 2 .

## OR

I used my calculator to find that it would take about 2 hours to stuff a total of 2604 envelopes. In my calculator I entered $672+720$ and got 1392 . I then did $2604 \div 1392$ and it gave me an answer of 1.87 . I rounded this number up to 2 .
\(\left.$$
\begin{array}{|c|l|}\hline \text { Score Point } & \text { Response Attributes } \\
\hline \mathbf{3} & \text { All is correct. } \\
\hline \mathbf{2} & \begin{array}{l}\text { All logic(s) or explanation(s) are correct. } \\
\text { Two correct logics or explanations and correct answers for two } \\
\text { problems or drawings. } \\
\text { OR }\end{array}
$$ <br>

One correct logic or explanation and correct answers for all problems.\end{array}\right\}\)| One or more answers to problems are correct. |
| :--- |
| OR correct logic or explanation. |

## ARMT GRADE 6 MATHEMATICS

## 3. Sample Response(s):

a. Harper's Restaurant: $\$ 5 \times 25=\$ 125 ; 0.15 \times \$ 4000=\$ 600 ; \$ 125+\$ 600=\$ 725$ OR
I used my calculator and multiplied 5 times 25 to get $\$ 125$. Then I multiplied 4000 times $15 \%(0.15)$ to get $\$ 600$. I then added $\$ 125$ and $\$ 600$ for a total of $\$ 725.00$.

## OR

First, I multiplied 5 times 25. This gave me $\$ 125$. After that, I multiplied 4000 times $15 \%$ and got an answer of $\$ 600$. Then, I added the two answers ( $\$ 125$ and $\$ 600$ ) and got a total answer of $\$ 725.00$. The food server made $\$ 725.00$ for the week.
b. Bea's Fine Dining: $\$ 8 \times 25=\$ 200 ; 0.12 \times \$ 4000=\$ 480 ; \$ 200+\$ 480=\$ 680$

## OR

I used my calculator and multiplied 8 times 25 to get $\$ 200$. Then, I multiplied 4000 times $12 \%(0.12)$ to get $\$ 480$. I then added $\$ 200$ and $\$ 480$ for a total of $\$ 680.00$.

## OR

First, I multiplied 8 times 25. This gave me $\$ 200$. After that, I multiplied 4000 times $12 \%$ and got an answer of $\$ 480$. Then, I added the two answers (\$200 and $\$ 480$ ) and got a total answer of $\$ 680.00$. The food captain made $\$ 680.00$ for the week.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | Two logics and explanations are correct. <br> OR |
| $\mathbf{1}$ | One correct logic or explanation and correct answer to both problems. <br> One answers to problems are correct. <br> OR |
| $\mathbf{0}$ | None is correct. (Also, blanks, rewrites problem, foreign language, <br> illegible, refusals, off task, etc., scored as invalid.) |

## ARMT GRADE 6 MATHEMATICS

## 4. Sample Response(s):

a. $\frac{30}{10}=\frac{30-21}{x}=\frac{9}{x} ; 30 x=90, x=3 ; 10-3=7$. Ally gave Louise 7 beads.

There are 30 red beads and 10 gold beads. This is a 3 to 1 ratio of red to gold beads. Since Ally had 21 gold beads, she would have to give Louise 7 gold beads to keep the same 3 to 1 ratio.

## OR

I set up a proportion and used my calculator to solve the problem. The answer from my proportion was 3 . Since there were 10 gold beads, I subtracted 3 and got 7 .
b. $30-21=9$ red beads left
$10-7=3$ gold beads left
OR
Ally started with 30 red beads, gave 21 away, so she had 9 red beads left. Ally started with 10 gold beads, gave 7 away, so she had 3 gold beads left. OR
I used my calculator to subtract 21 from 30 to get 9 red beads left and 7 from 10 to get 3 gold beads left.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | Two logics or explanations are correct. |
| $\mathbf{O n e}$OR correct logic or explanation and correct answer to two or more <br> problems. |  |
| $\mathbf{1}$ | Correct answers to one or more problems or drawings. <br> OR |
| $\mathbf{0}$ | One correct logic or explanation. |
| illegible, refusals, off task, etc., scored as invalid.) |  |

## ARMT GRADE 6 MATHEMATICS

## 5. Sample Response(s):

a. $\$ 500 \times 0.04=\$ 20 ; \$ 500+\$ 20=\$ 520$

## OR

On my calculator, I multiplied 500 times 0.04 . Then, I took the answer and added $\$ 500$ to get a total of \$520.

## OR

First, I multiplied 500 times 0.04 . This gave me an answer of 20 . Then, I added 20 to 500 and got an answer of $\$ 520$. This is how much money that was in the account after one year.
b. To calculate the amount of money Georgie had after 4 years:
after 1 year she had $500 \times 0.04=20 ; 500+20=520$
after 2 years she had $520 \times 0.04=20.80 ; 520+20.80=540.80$
after 3 years she had $540.80 \times 0.04=21.63 ; 540.80+21.63=562.43$
after 4 years she had $562.43 \times 0.04=22.50 ; 562.43+22.50=584.93$
OR
First, I took the answer for the amount of money that was in the account after one year ( $\$ 520$ ) and multiplied it times 0.04 . Then, I added $\$ 520$ to that answer and got an answer of $\$ 540.80$. $\$ 540.80$ is the amount in the account after 2 years. To find out how much money was in the account after 3 years, I took $\$ 540.80$ and multiplied it times 0.04 to get $\$ 21.63$. I added $\$ 540.80$ and $\$ 21.68$ to get an answer of $\$ 562.43$. To find out how much was in the account after 4 years, I took the year 3 answer of $\$ 562.43$ and multiplied it by 0.04 for an answer of $\$ 22.50$. Add $\$ 562.43$ and $\$ 22.50$ for a final answer of $\$ 584.93$.

## OR

I used a calculator to find the amount in the account after 4 years. I first took the answer from part a and kept multiplying the answer I got by 1.04, 3 times, until I got an answer of \$584.93.
c. The amount of money earned in interest each year was different. For year one it was $\$ 20$; for year two it was $\$ 20.80$; for year three it was $\$ 22.43$, and for year four it was $\$ 22.50$.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | All logic(s) or explanation(s) are correct. <br> OR |
| $\mathbf{1}$ | Two correct logics or explanations and correct answer for two problems <br> OR correct logic or explanation and correct answers for all problems. |
| $\mathbf{0}$ | One or more answers to problems are correct. <br> OR correct logic or explanation. |
| illegible, refusals, off task, etc., scored as invalid.) |  |

## ARMT GRADE 6 MATHEMATICS

## 6. Sample Response(s):

a. $\$ 1500 \times 0.06=\$ 90 ; \$ 1500+\$ 90=\$ 1590$

OR
On my calculator, I multiplied 1500 times 0.06 and got an answer of 90 . After that, I added 1500 to 90 and got a final answer of $\$ 1590$.

## OR

To calculate the simple annual interest for one year, I multiplied 1500 times 0.06 to get 90 . Then I added 90 to 1500 and got an answer of $\$ 1590$.
b. $\$ 1590 \div 12=\$ 132.50$

## OR

On my calculator, I divided $\$ 1590$ by 12 to get $\$ 132.50$ OR
To calculate the amount paid each of 12 months, I divided
$\$ 1590$ by 12. The amount of money paid back each month for 12 months was $\$ 132.50$.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | Two logics or explanations are correct. <br> OR |
| $\mathbf{1}$ | Error in logic or explanation and correct answers to two problems or <br> drawings. $\quad$OR <br> Correct answers to one or two problems or drawings. <br> OR |
| $\mathbf{0}$ | One correct logic or explanation. <br> None is correct. (Also, blanks, rewrites problem, foreign language, <br> illegible, refusals, off task, etc., scored as invalid.) |

## ARMT GRADE 6 MATHEMATICS

## 7. Sample Response(s):

a. Year 1: $600 \times 0.04=24 ; 600+24=624$

Year 2: $624 \times 0.04=24.96 ; 624+24.96=648.96$
Year 3: $648.96 \times 0.04=25.96 ; 648.96+25.96=674.92$.
It will take 3 years to have over 650 employees.

## OR

I have to find the amount of employees after each year and then find $4 \%$ of that number before calculating the next year. Take 600 and multiply it by 0.04 to get 24. Add 24 to 600 . Take 624 and multiply it by 0.04 to get 24.96 and add that to 624. Take 648.96 and multiply it times 0.04 to get 25.96 . Once you add 648.96 and 25.96 that is over 650 , so three years is the amount of time it will take for this company to have over 650 employees.

## OR

I used my calculator to find that it will take three years to have over 650 employees. Take 600 and multiply that by 0.04 and add that answer to 600 . Continue to take your answer and multiply it by 0.04 until you get at least 650 .
b. Year 1: $600 \times 0.08=48 ; 600+48=648$

Year 2: $648 \times 0.08=51.84 ; 648+51.84=699.84$
It will take 2 years to have over 650 employees.

## OR

To calculate the amount of time before there are 650 employees, I have to find the amount of employees after one year and then find $8 \%$ of that number before calculating the next year. For the first year, take 600 and multiply it by 0.08 for an answer of 48. Add 48 to 600, and take that answer and multiply it again by 0.08 for an answer of 51.84 . Add 51.84 to 648 for a total of 699.84 . It will take two years to have over 650 people.

OR
I used my calculator to find that it will take two years to have over 650 employees. Take 600 and multiply that by 0.08 . Then, add that answer to 600 . Continue to take your answer and multiply it by 0.08 until you get at least 650 .

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | Two logics or explanations are correct. <br> OR |
| $\mathbf{1}$ | Ene correct logic or explanation and correct answer to both problems. <br> drawings. $\quad$OR or explanation and correct answers to two problems or <br> Correct answers to one or two problems or drawings. <br> OR <br> One correct logic or explanation. |
| $\mathbf{0}$ | None is correct. (Also, blanks, rewrites problem, foreign language, <br> illegible, refusals, off task, etc., scored as invalid.) |

## ARMT GRADE 6 MATHEMATICS

## 8. Sample Response(s):

a. $\frac{20}{25}=0.80=80 \%$

OR
To calculate the percent of scores that were 7.0 or higher, I counted 20 scores, and divided by the total number of scores.
So, $\frac{20}{25}=0.80$ which is $80 \%$.

## OR

I used my calculator to divide 20 by 25 for an answer of 0.8 which is $80 \%$.
b. $\frac{21}{25}=0.84=84 \%$ that did not receive a blue ribbon.

OR
To calculate the percentage of gymnasts that did not receive a blue ribbon, count the number of scores in the $9.0-10.0$ range, which is 4 scores. Subtract that from the total number of scores which is 25 scores $(25-4=21)$. Take 21 and divide by the total number of scores. So, $\frac{21}{25}=0.84$ which is $84 \%$.

OR
I used my calculator to divide 21 by 25 for an answer of 0.84 or $84 \%$.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | Two logics or explanations are correct. <br> One correct logic or explanation and correct answer to one or more <br> problems. |
| $\mathbf{1}$ | Error in logic or explanation and correct answers to two problems or <br> drawings. $\quad$OR <br> Correct answers to one or two problems or drawings. <br> OR |
| $\mathbf{0}$ | One correct logic or explanation. <br> None is correct. (Also, blanks, rewrites problem, foreign language, <br> illegible, refusals, off task, etc., scored as invalid.) |

## ARMT GRADE 6 MATHEMATICS

## 9. Sample Response(s):

a. $\$ 900-\$ 720=\$ 180$

OR
On my calculator, I subtracted 720 from 900 to get 180 .

## OR

To find the amount of decrease from $\$ 900$ to $\$ 720$, subtract, $\$ 900-\$ 720=\$ 180$.
b. $\frac{180}{900}=0.20$ or $20 \%$.

OR
On my calculator, I first divided the amount of change (180) by the original amount (900). After that, I converted the answer (0.20) into a percent to get $20 \%$.

OR
To find the percent of change, divide the amount of change by the original amount, then convert to a percent. So, $\frac{180}{900}=0.20$ or $20 \%$.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | All logic(s) or explanation(s) are correct. <br> OR |
| $\mathbf{1}$ | One correct logic or explanation and correct answers for all problems. |
| One correct logic or explanation. |  |
| $\mathbf{0}$ | None is correct. (Also, blanks, rewrites problem, foreign language, <br> illegible, refusals, off task, etc., scored as invalid.) |

## ALGEBRA

## Content Standard 3

Solve problems using numeric and geometric patterns.

## Item Type

Multiple-choice
Gridded

## Additional Information

Determining a rule may be required.
Tables and charts may be used.
Work problems and problems in context may be used.

## Sample Multiple-Choice Items

1. The table below shows the amount of money Susan collected for a charity each week.

Susan's Collections

| Week | Amount Collected |
| :---: | :---: |
| 1 | $\$ 5$ |
| 2 | $\$ 12$ |
| 3 | $\$ 19$ |
| 4 | $\$ 26$ |

If the pattern shown in the table continued to increase by the same amount each week, how much should Susan have collected for charity in the ninth week?
\$33 \$40
\$47
\$61
A
B
C
D*
3. Travis started the pattern shown below.


If the pattern of taking away one side continues as shown, how many sides should the 5 th figure have?

| 14 | 6 | 4 | 1 |
| :--- | :--- | :---: | :---: |
| A | B | C* | D |

4. Elizabeth started the pattern shown below.


Which of the following should Elizabeth have drawn as the second figure?


A


B*


C


D
5. Arthur started this add 3 pattern.


If the pattern continues as shown, which of these should Arthur have drawn as the next figure?


A


B*


C


D
6. Victor started this doubling pattern.
$\bullet$

-     - 


$\begin{array}{ll}0 & 0 \\ 0 & 0\end{array}$

If the pattern continues as shown, how many dots should Victor draw in the next figure?
10
12
16
24
A
B
C*
D
7. The table below shows the number of cars Mario bought and the total amount spent. Each toy car has the same value.

Mario's Toy Cars

| Number of <br> Cars | Total Cost in <br> Dollars |
| :---: | :---: |
| 5 | $\$ 4.50$ |
| 10 | $\$ 9.00$ |
| 15 | $\$ 13.50$ |

If the pattern continued as shown in the table, what would be the total cost of 21 of these toy cars?
9. A pattern with differences is shown below.

Original Pattern


What should be the next term in the original pattern if the difference continues to increase at a constant rate?

| 160 | 170 | 180 | 190 |
| :--- | :--- | :--- | :--- |

8. Jordan started the number pattern below.
$0.489,0.448,0.407,0.366$,
If the pattern continues as shown, which of the following rules should he use to find the next term in the number pattern?

A Subtract 0.041*
B Add 0.041
C Add 0.41
D Subtract 0.41

## ARMT GRADE 6 MATHEMATICS

## Sample Gridded Items

1. A local radio station plans to give away 2 concert tickets on Monday, 6 concert tickets on Tuesday, and 18 concert tickets on Wednesday.

If this pattern continues, how many concert tickets will the radio station give away on Friday?

Mark your answer in the answer grid.
2. A pattern of $\mathbf{3 1}$ shapes appears on the border of an office building. The first 4 shapes of the pattern are shown below.


If the $\mathbf{4}$ shapes above keep repeating in this order, how many triangles are in the pattern?

Mark your answer in the answer grid.
3. Ashley's school collected pennies for 8 days to fund a college scholarship. On the first day, Ashley brought 1 penny, the second day she brought 2 pennies, the third day she brought 4 pennies, and the fourth day she brought 8 pennies.

If the pattern continued with the number of pennies doubling on each consecutive day, how many pennies did Ashley bring in all after 8 days?

Mark your answer in the answer grid.
4. Jesse decorated an award plaque by drawing a pattern of geometric figures. The first 5 shapes of his pattern are shown below.


If Jesse repeats the pattern in the order shown until there are $\mathbf{1 3}$ squares and 14 triangles, how many figures did he draw in his entire pattern?

Mark your answer in the answer grid.
5. Jared arranged his 44 sports cards in a pattern. Each sports card had a picture of a baseball player, football player, hockey player, or basketball player. The first 11 sports cards in the pattern are shown below.


If the $\mathbf{1 1}$ sports cards above kept repeating in this order, how many of Jared's sports cards had a picture of a hockey player?

Mark your answer in the answer grid.

# ARMT GRADE 6 MATHEMATICS 

## Answer Key

## Content Standard 3

Sample Multiple-Choice

1. D
2. D
3. C
4. B
5. B
6. C
7. C
8. A
9. B

## Sample Gridded

1. 162
2. 8
3. 255
4. 34
5. 16

## ARMT GRADE 6 MATHEMATICS

## GEOMETRY

## Content Standard 4

Identify two-dimensional and three-dimensional figures based on attributes, properties, and component parts.

## Item Type

Multiple-choice

## Additional Information

Matching a net to a three-dimensional figure may be required.
Diagrams of two-dimensional figures or three-dimensional figures may be used.
Word problems/real-life situations may be used.

## Sample Multiple-Choice Items

1. Gretta drew the figure below.


Which of these names the figure Gretta drew?

A Rectangular prism
B Triangular prism
C Triangular pyramid
D Square pyramid*
2. A net of a three-dimensional figure is shown below. A net is a pattern to be cut and folded to make a solid shape.


Which of these figures could be formed if the net was folded along the dotted line segments?

A Cube *
B Triangular pyramid
C Rectangular pyramid
D Triangular prism
3. Which regular figure has only 6 congruent angles?
A Triangle
C Hexagon*
B Pentagon
D Octagon
4. Which figure always has 4 congruent sides and exactly 2 sets of parallel sides?
A Trapezoid
C Rhombus*
B Rectangle
D Parallelogram
5.


Which figure shows this solid unfolded on a flat surface?
A

C

B*

D

6. Which of the following figures is an octagon?
A

C

B

D*

7. Lyle designed a garden so that it had seven equal sides.

Which figure has exactly 7 sides of equal length?

A A regular pentagon
B A regular heptagon*
C A regular nonagon
D A regular decagon
8. Which of the following figures always has 4 congruent sides?

A Isosceles trapezoid
B Parallelogram
C Rectangle
D Rhombus*
10. Which of the following twodimensional figures has exactly 5 sides?
A Parallelogram
C Hexagon
B Pentagon*
D Octagon
9. Which of these appears to be a square pyramid?
A

C

B

D*

11. Henry cut a piece of cardboard into differentshaped pieces. One of the pieces had exactly 2 sets of parallel sides and 4 congruent angles.

Which could be one of the pieces Henry cut?

A A trapezoid
B A rhombus
C A square*
D A pentagon
12. Alyssa drew the picture of the three-dimensional figure below.


Which of the following names the figure Alyssa drew?

A Cone*
B Cylinder
C Pyramid
D Sphere
13. Gabriella drew a picture of a swimming pool. The swimming pool had five sides.

Which is the shape of the swimming pool she drew?
14. Which of these appears to be a triangular pyramid?
A

C

B*

D

15. Albert drew several threedimensional figures.

Which of the following figures had exactly 5 faces and 5 vertices?

A Triangular pyramid
B Triangular prism
C Rectangular pyramid*
D Rectangular prism

A Pentagon*
B Parallelogram
C Trapezoid
D Hexagon

## ARMT GRADE 6 MATHEMATICS

## Answer Key

## Content Standard 4

## Sample Multiple-Choice

1. D
2. $\mathbf{A}$
3. C
4. $C$
5. B
6. D
7. B
8. D
9. D
10. B
11. C
12. A
13. A
14. B
15. C

## GEOMETRY

## Content Standard 5

Plot coordinates on grids, graphs, and maps.

## Item Type

Multiple-choice

## Additional Information

Identifying coordinates of a point on a grid, graph, or map may be required.
Following directions to locate a point on a grid, graph, or map may be used.
Using ordered pairs to represent the location of a point on a grid, graph, or map may be used.
Identifying coordinates of a point on the coordinate plane may be required.
Real-life situations may be included.

## Sample Multiple-Choice Items

1. The location of the campsite is shown on the grid.


The swimming pool is located two blocks east and one block south of the campsite.
What is the location of the pool?
C-2
C-6
D-3
D-5
A
B
C*
D

## ARMT GRADE 6 MATHEMATICS

2. Beverly graphed 4 points on the grid below.


Which of the following points best represents the coordinates ( $-1,4$ )?

| $T$ | $U$ | $V$ | $Z$ |
| :---: | :---: | :---: | :---: |
| A | B | $\mathbf{C}^{*}$ | D |

## ARMT GRADE 6 MATHEMATICS

3. The grid below shows the location of Mr. Lang's classroom.


Which best represents the coordinates of Mr. Lang's classroom?
$(3,4)$
$(3,-4)$
A
B*
$(-4,3)$
C
$(4,3)$
D

## ARMT GRADE 6 MATHEMATICS

4. 



Which point on the grid is best represented by the ordered pair (7, 2)?

| $H$ | $J$ | $K$ | $L$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ | $\mathbf{D}^{*}$ |

## ARMT GRADE 6 MATHEMATICS

5. Kendra graphed point $K$ on the grid below.


Which ordered pair best represents the location of point $K$ ?
$(6,-4)$
$(-4,6)$
$(6,4)$
$\left(-4,{ }^{-6}\right)$
A*
B
C
D

## ARMT GRADE 6 MATHEMATICS

6. The location of Earl's garden in the community garden is shown on the grid below.


Community Garden Plots


Diane's garden plot is located 3 units north and 1 unit west of Earl's garden plot. Which point best represents the location of Diane's garden?
D-5
F-5
A*
B
G-4
H-3
B
C
D

## ARMT GRADE 6 MATHEMATICS

7. The letters on the grid below represent the different places Doug needs to go to help him locate items in a scavenger hunt.


Which of the following letters is located at $\left(5,{ }^{-} 1\right)$ on the grid?

| $U$ | $R$ | $S$ | $T$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ | $\mathbf{D}^{*}$ |

## ARMT GRADE 6 MATHEMATICS

8. The grid below shows the location of $\mathbf{4}$ vertices of a square.


Which vertex of the square is located at point $\left(5,,^{-2}\right)$ on the grid?
$T$
U
V
A
B
C*
W
-

## ARMT GRADE 6 MATHEMATICS

## Answer Key

## Content Standard 5

## Sample Multiple-Choice

1. C
2. C
3. B
4. D
5. A
6. A
7. D
8. C

## MEASUREMENT

## Content Standard 6

Classify angles as acute, obtuse, right, or straight.

## Item Type

Multiple-choice

## Additional Information

A diagram may be included.
Pictures of real-life objects may be included.
Drawing an angle on a grid may be required.

## Sample Multiple-Choice Items


3. Which of the following angles best represents a right angle?

A


B


C*


D

4. Riley rode her bicycle west on Main Street and made a 75-degree turn at Elm Street.

What kind of angle represents the $75^{\circ}$ turn Riley made at Elm Street?
A Straight
C Obtuse
B Right
D Acute*
5. The picture below shows a magnet of the letter " $A$ ".


What type of angle does $\boldsymbol{U}$ appear to be?
A Acute
C Right
B Obtuse*
D Straight

## ARMT GRADE 6 MATHEMATICS

6. 



What type of angle does each of the figures above have in common?

Straight
A
Right

B
Obtuse
C
Acute
D*
7. A picture of a ruler is shown below.


What type of angles do the corners of the ruler appear to be?

| Acute | Right | Obtuse | Straight |
| :---: | :---: | :---: | :---: |
| A | B $^{*}$ | C | D |

## ARMT GRADE 6 MATHEMATICS

8. Stop signs are constructed in the shape of regular octagons.

Which of the following angles are at the vertices of a regular octagon?
A Acute
C Right
B Obtuse*
D Straight
9. Which type of angle is formed by connecting line segments $M A$ and $A T$ using point $A$ as the vertex?

A Acute
C Obtuse*
B Right
D Straight


## ARMT GRADE 6 MATHEMATICS

## Answer Key

## Content Standard 6

## Sample Multiple-Choice

1. C
2. D
3. C
4. D
5. B
6. D
7. B
8. B
9. C
10. A
11. A

## MEASUREMENT

## Content Standard 7

Solve problems involving perimeter and area of parallelograms and rectangles.

## Item Type

Multiple-choice
Gridded
Open-ended

## Additional Information

Determining a missing measurement when given the area or perimeter of a parallelogram or a rectangle may be required.
Determining either the area or the perimeter of a parallelogram or a rectangle given either the area or the perimeter of the figure may be required.
Diagrams may be used.
Determining the area or perimeter of a shaded part of a figure may be required.
Word problems/real-life situations and problems in context may be used.
A comparison of figures may be required.

## Sample Multiple-Choice Items

1. The front of the door to Rueben's classroom is a rectangle with an area of 2688 square inches.

If the width of the front of the door is 32 inches, what should be the measure of the height?

640 inches
A

116 inches
B
84 inches
C*

42 inches
D
2. The area of a parallelogram is 16 square meters. The base of the parallelogram is $\mathbf{8}$ meters.

What is the height, in meters, of the parallelogram?

| 2 | 8 | 24 | 128 |
| :---: | :---: | :---: | :---: |
| $\mathbf{A}^{*}$ | $\mathbf{B}$ | $\mathbf{C}$ | $\mathbf{D}$ |

3. The perimeter of a square is 20 centimeters.

What is the area?
A 5 sq cm
C 30 sqcm
B 25 sq cm *
D 400 sq cm
4. The perimeter of a rectangle is 54 inches. The width of the rectangle is $\mathbf{8}$ inches.

What is the length of the rectangle?
A 16 inches
C 38 inches
B 19 inches*
D 46 inches
5. A diagram of an exercise mat is shown below.


8 feet

The width of the mat is $\frac{1}{2}$ the length.

What is the perimeter of the exercise mat in feet?
A 4 feet
C 24 feet*
B 9 feet
D 32 feet
6. What is the area of the parallelogram shown below?

A $8.8 \mathrm{~m}^{2}$
C $19.0 \mathrm{~m}^{2 *}$
B $\quad 17.6 \mathrm{~m}^{2}$
D $38.0 \mathrm{~m}^{2}$
7. What is the area of a parallelogram with a width of 13.9 centimeters and a height of 22.4 centimeters?
A $36.3 \mathrm{~cm}^{2}$
C $72.6 \mathrm{~cm}^{2}$
B $68.6 \mathrm{~cm}^{2}$
D $311.36 \mathrm{~cm}^{2}$ *
8. A poster on Evan's wall is 24 inches wide and $18 \frac{1}{4}$ inches high. On the top of the poster is a $3 \frac{1}{4}$ inch heading.


What is the perimeter of the poster without the heading?
A 84 inches
C 74 inches
B 78 inches*
D 68 inches

## ARMT GRADE 6 MATHEMATICS


A 48 square feet
C 103 square feet*
B 50 square feet
D 143 square feet

## ARMT GRADE 6 MATHEMATICS

## Sample Gridded Items

1. The bottom of the cage where Alex keeps his pet mouse is in the shape of a rectangle with a perimeter of 58 inches. The length of the bottom of the cage is $\mathbf{1 8 . 3}$ inches.

What is the width of the bottom of the cage?

Mark your answer in the answer grid.
2. Sandy removed two small pieces from the large rectangle shown below.


What is the area, in square inches, of the remaining part of the original rectangle?
3. What is the perimeter of the figure shown below in meters?


Mark your answer in the answer grid.

Mark your answer in the answer grid.

## ARMT GRADE 6 MATHEMATICS

4. What is the perimeter, in centimeters, of the figure shown below?


Mark your answer in the answer grid.
5. The layout of Tim's house is rectangular and the lawn around it is also rectangular.


What is the area, in square feet, of the lawn?

Mark your answer in the answer grid.

## Sample Open-Ended Items

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.

1. Malcolm was given a piece of grid paper in art class and was asked to make a design with different figures. The design he made is shown below.


$$
\text { Scale: } 1 \square=1 \text { square inch }
$$

a. Identify the gray, shaded geometric figures in Malcolm's design.
b. How much gray material will be used in Malcolm's design?
c. How much white material will Malcolm need for the design?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
2. The top of the Traeger family's kitchen table is square. The Reyes family's kitchen tabletop is rectangular. The perimeter of each tabletop is $\mathbf{1 8}$ feet.
a. Draw and label an outline of the top of the Traeger's table.
b. Draw and label one possible outline of the top of the Reyes's table.
c. Which table has the greatest area?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
3. The 6th grade class at Garner Valley Middle School is planning a social event. The students on the decorating committee will use this template design to make the invitations. Each grid square is equal to 1 square inch. The invitations will be gray and white.

a. Identify the gray, shaded geometric figures in the design.
b. How much gray space is used in the invitation?
c. How much white space is used in the invitation?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
4. Coach Savitz is having a design painted, in gray and white paint, on the soccer field as shown below. The design will be based on the drawing on this 15 by 15 grid.

Coach Savitz's Design


Scale: $\square=1$ Square foot
a. Identify the gray geometric figures in Coach Savitz's design.
b. How much gray area will be painted in Coach Savitz's design?
c. How much white area will be painted in Coach Savitz's design?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
5. Gina is making the base of a model using toothpicks. The base resembles the letter " $T$ ". Each toothpick is equal to 3 units, so the figure has several squares, each 3 units by 3 units.

a. Find the perimeter in units of Gina's figure.
b. Find the area in square units of Gina's figure.
c. If one of the $\mathbf{3}$ by $\mathbf{3}$ squares were moved to a different location than shown on Gina's drawing, would the area, perimeter, or both change or stay the same?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
6.

a. What is the name of the four-sided figure shown in this grid?
b. How would you determine the area of this figure?
c. What is the area of this figure if every grid square represents 1 square meter?

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

# ARMT GRADE 6 MATHEMATICS 

## Answer Key

## Content Standard 7

## Sample Multiple-Choice

1. C
2. $\mathbf{A}$
3. B
4. B
5. C
6. C
7. D
8. B
9. C
10. C
11. A

## Sample Gridded

1. 10.7
2. 98.7
3. 132
4. 76
5. 5800

## ARMT GRADE 6 MATHEMATICS

## Sample Open-Ended

## 1. Sample Response(s):

a. It is made up of 4 rectangles and 1 parallelogram.
b. The area of the parallelogram is $6 \times 3=18$. Each "L" shape is made up of 2 rectangles. I separated them into a $12 \times 3$ rectangle and a $2 \times 4$ rectangle. Therefore, the area of one "L" shape is $36+8=44$. Since there are 2 "L" shapes, that would be 88 square inches. The amount of gray material that will be used is $18+88=106$ square inches.

## OR

Area of Parallelogram: $6 \times 3=18$
Area of Rectangles ("L" shapes): $2(12 \times 3+2 \times 4)=88$
Add the two areas together to get: 106 square inches of gray material.

## OR

106 square inches of gray material. I used my calculator to find the area of each section of the rectangles (the "L" shapes) and the area of the parallelogram.
c. $225-106=119$ square inches of white material.

OR
There are a total of 225 squares. 106 of the squares are the gray material.
Therefore, $225-106=119$ square inches of the white material.
OR
I used my calculator to find the total area of the template to be 225 square inches. I took the answer from part b and subtracted it from 225. The answer is 119 square inches of white material.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | Two logics or explanations are correct. <br> OR |
| $\mathbf{1}$ | One correct logic or explanation and correct answer to at least B and C. <br> drawings. Or in logic or explanation and correct answer to two problems or <br> Correct answers to one or two problems or drawings. <br> OR |
| $\mathbf{0}$ | One correct logic or explanation. |
| None correct. (Also, blanks, rewrites problems, foreign language, |  |
| illegible, refusals, off task, etc., scored as invalid.) |  |

## ARMT GRADE 6 MATHEMATICS

## 2. Sample Response(s):

a. To find the Traeger's tabletop, $18 \div 4=4.5$. The square tabletop has dimensions of 4.5 inches by 4.5 inches.

b. The Reyes's tabletop, with perimeter 18 , is 5 inches by 4 inches, so that $5+4+5+4=18$.

c. The Traeger's tabletop has an area of 4.5 feet $\times 4.5$ feet $=20.25$ feet squared. The Reyes's tabletop has an area of 5 feet $\times 4$ feet $=20$ feet squared. The Traeger's tabletop has the greater area.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |

## ARMT GRADE 6 MATHEMATICS

## 3. Sample Response(s):

a. The gray sections are parallelograms.
b. The area of each parallelogram is $8 \times 4=32$. There are 2 parallelograms, so $32 \times 2=64$.

## OR

Each gray section has an area of 32 square inches. Since there are 2 parallelograms with the same area, the total to be cut off is 64 square inches.

## OR

64 square inches. I used my calculator to find the area of each parallelogram, and when I found the area of one parallelogram, I multiplied it by 2 because there are 2 parallelograms.
c. $144-64=80$ square inches.

## OR

There are a total of 144 squares and 64 will be cut off, so $144-64=80$. 80 squares will be used.

## OR

I used my calculator to find the total area of the template to be 144 square inches. I took the answer from part b and subtracted it from 144. The answer is 80 square inches.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | All logic(s) or explanation(s) are correct. <br> OR |
| Two correct logics or explanations and correct answer to at least part b <br> and part c. $\quad$ OR <br> One correct logic or explanation and correct answers for all problems. |  |
| $\mathbf{1}$ | One or more answers to problems are correct. |
| $\mathbf{0}$ | None correct. (Also, blanks, rewrites problem, foreign language, <br> illegible, refusals, off task, etc., scored as invalid.) |

## ARMT GRADE 6 MATHEMATICS

## 4. Sample Response(s):

a. The figure is made up of a rectangle and a parallelogram.
b. Rectangle: $9 \times 3=27$

Parallelogram: $11 \times 4=44$
$27+44=71$ square feet

## OR

The rectangle is $9 \times 3=27$ feet squared, and the parallelogram has an area of $11 \times 4=44$ feet squared, so $27+44=71$ feet squared.

## OR

I used my calculator to find the area of the rectangle and the area of the parallelogram for a total of 71 square feet.
c. $15 \times 15=225$
$225-71=154$ square feet
OR
The total area of the grid is 225 square inches. Take the answer from part b and subtract it from 225 . The area of the white area is 154 square feet.

OR
I used my calculator to find the total area of the grid and subtracted the gray area to get 154 square feet.
$\left.\begin{array}{|c|l|}\hline \text { Score Point } & \text { Response Attributes } \\ \hline \mathbf{3} & \text { All is correct. } \\ \hline \mathbf{2} & \begin{array}{l}\text { All logic(s) or explanation(s) are correct. } \\ \text { OR }\end{array} \\ \hline \mathbf{T} \text { Two correct logics or explanations and correct answer to at least part b } \\ \text { and part c. OR } \\ \text { One correct logic or explanation and correct answers for all problems. }\end{array}\right\}$

## ARMT GRADE 6 MATHEMATICS

## 5. Sample Response(s):

a. The perimeter is 36 units. $3+3+6+3+6+3+3+9=36$.
b. I split the "T" into two rectangles. The area of one rectangle is $3 \times 9=27$ square units plus the area of the other rectangle is $3 \times 6=18$. Rectangle one plus rectangle two equals 45 square units.
c. No matter where you moved one $3 \times 3$ square to another part of the figure the area would stay the same if no overlapping of squares occurred.

The answer for perimeter depends on which square you move. The perimeter could stay the same or be different than 36 units. In one case, I moved the right side of the top part of the " T " underneath the lower left side of the " T " and it changed the perimeter to 30 .

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |

## ARMT GRADE 6 MATHEMATICS

## 6. Sample Response(s):

a. Rectangle
b. To get the area of this figure, you could count the number of blocks within the dark outline. You could also use the formula for a rectangle and count the number of blocks in the length of the figure, count the number of blocks in the width of the figure, and then multiply those two numbers together.
c. $7 \times 10=70$ square meters.

## OR

To find the area of the rectangle, multiply the length times the width. Length $=10$, Width $=7,10 \times 7=70$ square meters.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |

## MEASUREMENT

## Content Standard 8

Determine the distance between two points on a scale drawing or a map using proportional reasoning.

## Item Type

Multiple-choice
Gridded

## Additional Information

Determining the scale may be required.
Scale drawing may be included.
Word problems/real-life situations may be used.
Measuring a scale drawing may be required.

## Sample Multiple-Choice Items



## ARMT GRADE 6 MATHEMATICS

2. Use your centimeter ruler and this map to help you answer this question.

The dotted-line segment on the map shows the shortest distance from the beginning of a hiking trail to the end of a hiking trail.


Which is closest to the actual distance, in yards, represented by the dottedline segment?

| 500 | 5000 | 10,000 | 25,000 |
| :---: | :---: | :---: | :---: |
| A | $\mathbf{B}$ | $\mathbf{C}^{*}$ | $\mathbf{D}$ |

3. A scale drawing of a giraffe is shown below.

Giraffe


The scale used to create the drawing was 1 centimeter represents $\mathbf{3}$ feet. Using your ruler, determine the height of the actual giraffe.
6 centimeters $\quad 6.75$ feet $\quad 9$ centimeters 18 feet

A
B
C
D*

## ARMT GRADE 6 MATHEMATICS

4. A scale drawing of Anita's bedroom is shown below.


Anita used a scale of 1 centimeter represents 3 feet. Using your ruler, determine the actual dimensions of Anita's bedroom.
A $4 \frac{1}{2}$ centimeters by 6 centimeters
C $13 \frac{1}{2}$ feet by 18 feet*
B 9 feet by 12 feet
D $13 \frac{1}{2}$ meters by 18 meters

## ARMT GRADE 6 MATHEMATICS

5. The scale drawing of the aquarium below is $\frac{1}{16}$ the size of the original aquarium.


Using your ruler, determine the actual measurements of the shaded face of the aquarium.
A $2 \frac{1}{8}$ inches by $\frac{7}{8}$ inches
C $18 \frac{1}{8}$ inches by $16 \frac{7}{8}$ inches
B $5 \frac{1}{2}$ inches by $2 \frac{2}{10}$ inches
D 36 inches by 14 inches*

## ARMT GRADE 6 MATHEMATICS

6. The map below shows the locations of Madison School, Bartlett School, and Harper Library. $\frac{1}{2}$ inch $=2$ miles.


Using your inch ruler, what is the street distance, in miles, between Madison School and Harper Library?
2.75
4.75
7
11
A
B
C
D*

1. The floor plan of the Murphy home uses a scale of $\mathbf{1}$ inch to represent 4 feet.

If the actual length of the Murphy living room is $\mathbf{1 8}$ feet, what is the length, in inches, on the floor plan?

Mark your answer in the answer grid.
2. Harold and Danielle each drew a scale drawing of a monument. In Harold's drawing, the height of the monument was 15 centimeters and the width was 6 centimeters. Danielle's drawing of the monument was similar to Harold's. In Danielle's drawing, the height of the monument was 20 centimeters.

What was the width of the monument, in centimeters, in Danielle's scale drawing?

Mark your answer in the answer grid.

# ARMT GRADE 6 MATHEMATICS 

## Answer Key

## Content Standard 8

## Sample Multiple-Choice

1. A
2. C
3. D
4. C
5. D
6. D

Sample Gridded

1. 4.5
2. 8

## MEASUREMENT

## Content Standard 9

Convert units of length, weight, or capacity within the same system (customary or metric).

## Item Type

Multiple-choice

## Additional Information

Converting from a larger unit to a smaller unit may be required.
Converting from a smaller unit to a larger unit may be required.
Word problems/real-life situations may be used.

## Sample Multiple-Choice Items

1. Henry's fish tank has a capacity of 28 quarts of water.

How many gallons of water would it take to fill Henry's fish tank to capacity?
A 112 gallons
C 7 gallons*
B 28 gallons
D 4 gallons
2. A bridge has a weight limit of 16,000 pounds.

What is the weight limit, in tons, of this bridge?
A 2 gallons
C 2 quarts
B 2 fluid ounces
D 2 cups*
A 8 tons*
C 80 tons
B 16 tons
D 160 tons
5. Savannah is $\mathbf{1 5 5}$ centimeters tall.

Which of the following is equivalent to 155 centimeters?
A 0.0155 m
C 1.55 m *
B 0.155 m
D 15.5 m
6. A bag of pecans that Alexis wants to buy has a total weight of 54 ounces.

Which of the following is equivalent to 54 ounces?
A 6.75 pounds
C 2.25 pounds
B 3.375 pounds*
D 1.125 pounds
7. The package of crackers that Anna bought has a mass of 49 grams.

Which of the following is equivalent to $\mathbf{4 9}$ grams?
A 4.9 kg
C $0.049 \mathrm{~kg}^{*}$
B $\quad 0.49 \mathrm{~kg}$
D 0.0049 kg
8. Armando jumped over a puddle of water that was 76 inches wide.

Which of the following is equivalent, in feet, to the width of this puddle of water?
A $7 \frac{1}{2}$ feet
C $6 \frac{1}{4}$ feet
B $6 \frac{1}{3}$ feet*
D $1 \frac{1}{2}$ feet
9. The length of the earthworm that Timmy found in his back yard was 38 millimeters.

Which is equivalent to 38 millimeters?
A 0.038 cm
C 3.8 cm *
B 0.38 cm
D 380 cm
10. The phonebook for the city of Mapleton had a mass of 0.7 kilograms.

Which of the following is equivalent to 0.7 kilograms?
A 70 grams
C 7000 grams
B 700 grams*
D 70,000 grams
11. David made 9 liters of fruit punch.

Which of the following is equivalent to 9 liters?

A 0.9 milliliters
B 9 milliliters
C 90 milliliters
D 9,000 milliliters*
12. Which is equivalent to 308 meters?

A 3.08 centimeters
B 30.8 centimeters
C 3080 centimeters
D 30,800 centimeters*
14. Which is equivalent to 0.55 kilometers?
A $55,500 \mathrm{~cm}$
C 550 m*
B 5500 m
D 55 km
15. Miguel ordered a total of 18 gallons of milk for his grocery store.

Which of the following is equivalent to 18 gallons?

A 72 quarts*
B 144 cups
C 288 fluid ounces
D 2304 pints
13. Which is equivalent to 0.79 meters?

A 7.90 km
B $\quad 0.079 \mathrm{~km}$
C 0.00079 km *
D 0.0079 km

## ARMT GRADE 6 MATHEMATICS

## Answer Key

## Content Standard 9

Sample Multiple-Choice

1. C
2. $\mathbf{A}$
3. C
4. D
5. C
6. B
7. C
8. B
9. C
10. B
11. D
12. D
13. C
14. C
15. A

## DATA ANALYSIS AND PROBABILITY

## Content Standard 10

Interpret information from bar graphs, line graphs, and circle graphs.

## Item Type

Multiple-choice
Gridded
Open-ended

## Additional Information

Word problems/real-life situations may be used.
Comparing types of graphs may be required.
Determining percents may be required.
Money values may be used.

## Sample Multiple-Choice Items

1. The graph below displays the decibel level of a song after a specific number of seconds.


Which of the following is closest to the difference in the decibel level of the song between the 2 -second interval and the $\mathbf{6}$-second interval?
5
15
25
35
A
B
C*
D

## ARMT GRADE 6 MATHEMATICS

2. The graph shows the results of a survey about the favorite sport of a group of 300 students from Mr. Jahn's gym classes.


What was the total number of students in the group who chose football as their favorite sport?
33
75
99
150
A
B
C*
D

## ARMT GRADE 6 MATHEMATICS

## Sample Gridded Items

1. The graph below displays the sales amounts for puzzles over a number of years.


By how many dollars did the sales of puzzles increase from 1996 to 1998?

Mark your answer in the answer grid.
2. The line graph below displays the amount of flour needed in a muffin recipe.

Flour to Make Muffins


Based on this graph, what is the number of cups of flour needed to make 40 muffins?

Mark your answer in the answer grid.
3. The graph below displays the price of spiral notebooks at two different stores over a 12 -month period.


Which month appears to have had the least difference in price of spiral notebooks at the two stores?

Mark your answer in the answer grid.

## Sample Open-Ended Items

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.

1. In the school newsletter there is an article about the number of female students who participate in sports at the school. The data display shown in the article shows that softball is twice as popular among the female students as basketball.

a. Would you accept this data display and interpretation? Why or why not?
b. Draw a graph that would accompany the article. Explain why you chose this graph.

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
2. The number of oranges and apples sold at a produce stand are shown in this table.

|  | Number <br> Displayed | Number <br> Sold |
| :---: | :---: | :---: |
| Oranges | $\mathbf{7 0}$ | $\mathbf{3 5}$ |
| Apples | $\mathbf{9 0}$ | $\mathbf{6 3}$ |

Mrs. Valdez wants to use one of the graphs below to display the percent of oranges and apples she sold in her produce stand.

a. Does one bar graph more accurately present the data than the other bar graph?
b. In a sentence or two, state how the less accurate bar graph could be changed so that it would better represent the data in the table.

Show all your work and/or explain your reasoning for each part in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

This problem requires you to show your work and/or explain your reasoning. You may use drawings, words, and/or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning. It is important that you show all your work.
3. Both of the following data displays show the average monthly rainfall for one small town.


Which graph displays the data more accurately and why?

Show all your work and/or explain your reasoning in the space provided in the answer document.

## ARMT GRADE 6 MATHEMATICS

## Answer Key

## Content Standard 10

## Sample Multiple-Choice

1. C
2. C

Sample Gridded

1. \$150000 or \$150000.00 or 150000 or 150000.00
2.8
2. 8

## ARMT GRADE 6 MATHEMATICS

## Sample Open-Ended

## 1. Sample Response(s):

a. I would not accept this graphic, because the intervals make it visually misleading. The vertical axis does not start at zero and the difference between softball and basketball participation appears to be more substantial than it actually is.

A better representation would include a bar graph or a circle graph drawn to scale.
b.

Female Students Participate in Sports


Sport
I chose this graph to illustrate the information in the article, because a bar graph works well for this type of representation. In the original question, the vertical axis was wrong. It needs to start at zero as mine does, so that the graph does not look like softball is twice as popular as basketball.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | All logics or explanations are correct. <br> OR |
| $\mathbf{1}$ | One logic or explanation and graph are correct. |
| $\mathbf{0}$The graph has no more than three errors. <br> OR |  |
| $\mathbf{0}$ | None correct. (Also, blanks, rewrites problem, foreign language, <br> illegible, refusals, off task, etc., scored as invalid.) |

## ARMT GRADE 6 MATHEMATICS

## 2. Sample Response(s):

a. Graph 1 displays the data more accurately than Graph 2. Graph 2 is misleading, because the first interval on the $y$-axis is much larger than all the other intervals. This makes the number of oranges sold appear much closer to the number of oranges displayed.
b. How the student could possibly better the less accurate graph will vary. Students might possibly state that the vertical axis should have all the same sized intervals beginning at zero.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | All is correct. |
| $\mathbf{2}$ | The logic or explanation is correct for part a or part b. |
| $\mathbf{1}$ | Identify which is more accurate. |
| $\mathbf{0}$ | None correct. (Also, blanks, rewrites problem, foreign language, <br> illegible, refusals, off task, etc., scored as invalid.) |

## 3. Sample Response(s):

The graph on the right is more accurate than the graph on the left. The graph on the left does not begin with 0 on the vertical axis.

| Score Point | Response Attributes |
| :---: | :--- |
| $\mathbf{3}$ | Picked one and fully justified with logic to support the selection. |
| $\mathbf{2}$ | Picked one and did not fully support the selection. |
| $\mathbf{1}$ | Picked one with no supporting logic. |
| $\mathbf{0}$ | None correct. (Also, blanks, rewrites problem, foreign language, <br> illegible, refusals, off task, etc., scored as invalid.) |

## DATA ANALYSIS AND PROBABILITY

## Content Standard 11

Find the probability of a simple event.

## Item Type

Multiple-choice
Gridded

## Additional Information

Expressing probability as a fraction, decimal, or percent may be required.
Tables may be used.
Word problems/real-life situations may be used.
Diagrams may be included.

## Sample Multiple-Choice Items


2. The picture below represents Adrian's bag of marbles. All of the marbles are the same size and shape.


What is the probability that Adrian will not select a yellow or red marble, without looking, on his first try?

| $\frac{3}{10}$ | $\frac{7}{10}$ | $\frac{5}{16}$ | $\frac{5}{32}$ |
| :---: | :---: | :---: | :---: |
| A | B | C* | D |

3. Trudie is playing a game with identical-sized colored sticks. She has a container with a total of 10 red, 12 green, 19 blue, and 9 yellow sticks.

If Trudie picks a stick without looking, what is the probability the stick will be green?

12\% 24\% 76\% 88\%
A B* C $\quad$ D
4. There are 12 students playing a game that requires each one to pick a piece of paper from a hat. The pieces of paper are identical in size and on each of the pieces is the name of a different student playing the game.

What is the probability that a student will pick the piece of paper from the hat with his or her own name?
$\frac{1}{12}$
$\frac{6}{12}$
$\frac{7}{12} \quad \frac{8}{12}$
A* B $\quad$ C $\quad$ D

## ARMT GRADE 6 MATHEMATICS

## Sample Gridded Items

1. The spinner below is divided into 8 equal sections. Whitney spun the arrow on the spinner once.


If Whitney spins the arrow once, what is the probability that the spinner will not land on $T$ ?

Express your answer as a decimal.
2. Maryanne painted some identical-sized wooden blocks. She painted 6 green wooden blocks, 5 red wooden blocks, 4 blue wooden blocks, and 5 yellow wooden blocks and placed them in an empty bag.

If Maryanne then selects a wooden block from the bag without looking, what is the probability that it will be one that was painted red?

Express your answer as a decimal.

Mark your answer in the answer grid.

Mark your answer in the answer grid.
3. A citywide youth event had participants from 4 neighborhoods. There were 250 participants from Oak Bluff, 310 participants from Gordon Grove, 280 participants from Riverside, and 160 participants from Webster Heights.

If a participant is chosen at random to win a prize, what is the probability that the participant will be from Gordon Grove?

Express your answer as a decimal.

Mark your answer in the answer grid.
4. Brendan has $\mathbf{4 0}$ individual socks in his drawer. Of all the socks, 26 are dark blue.

If Brendan opens the drawer and selects one sock without looking, what is the probability that he will select a sock that is not dark blue?

Express your answer as a decimal.
5. Angela put colored paperclips into her empty pocket. She put 13 pink, 4 red, 1 yellow, and 2 green paperclips into her pocket. All of the paperclips are the same size and shape.

If Angela reaches into her pocket containing these colored paperclips and selects a paperclip, what is the probability it will be a green or yellow paperclip?

Express your answer as a decimal.

Mark your answer in the answer grid.

Mark your answer in the answer grid.

# ARMT GRADE 6 MATHEMATICS 

## Answer Key

## Content Standard 11

Sample Multiple-Choice

1. A
2. C
3. B
4. A

Sample Gridded

1. 0.875
2. 0.25
3. 0.31
4. 0.35
5. 0.15
