# **ACTAAP**

Arkansas Comprehensive Testing, Assessment, and Accountability Program

## RELEASED ITEM BOOKLET Algebra I End-of-Course Examinations 2011–2012 Administrations

#### **Arkansas Department of Education**

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- 1. What is the value of x if  $x = (7+9) \div (4-2)^2$ ?
  - A. 1
  - \* B. 4
    - C. 12
    - D. 16
- 2. Adele's lawn has an area of  $(x^2 5x 6)$ square feet and a length of (x+1) feet. What is the width of the lawn in feet?
  - \* A. (*x*-6)
    - B. (x+6)
    - C.  $(x^2 4x 5)$
    - D.  $(x^2 6x 7)$

- 3. Ana made a pizza with a circumference of  $16\pi$  in. What is the radius, in inches, of the pizza?
  - A. 0.13
  - \* B. 8
    - C. 16
    - D. 32



4. The scatter plots below show the average daily temperature for two **different** months.

Which statement about the data shown is true?

- A. The data for each graph will have a positive correlation.
- B. The data in the first graph was collected over a much greater time period.
- \* C. The range of the data for the second graph is greater than the first graph.
  - D. The median temperature for the first graph is higher than the second graph.

5. Which equation represents a line that passes through the points (4, 12) and (8, 9)?

A. 
$$y = \frac{3}{4}x + 3$$

B.  $y = -\frac{3}{4}x + 6$ 

C. 
$$y = -\frac{3}{4}x + 9$$
  
\* D.  $y = -\frac{3}{4}x + 15$ 

- 6. If  $a_n = 3n 2$ , what is the 15th term in the sequence?
  - A. 39
  - \* B. 43
    - C. 45
    - D. 47

7. Which is the factored form of the polynomial  $6x^2 + 7x - 5?$ 

\* A. 
$$(3x+5)(2x-1)$$
  
B.  $(2x+5)(3x-1)$   
C.  $(3x-5)(2x+1)$   
D.  $(2x-1)(3x-5)$ 

8. Consider these two events:

Event 1 — Devin sleeps through his alarm in the morning.

Event 2 — Devin misses the school bus.

Which of the following **best** describes the relationship between Event 1 and Event 2?

- \* A. causation
  - B. condition
  - C. correlation
  - D. combination

- 9. Which expression is equivalent to  $\sqrt{\frac{81}{72-8}}$ ?
  - \* A.  $\frac{9}{8}$ 
    - B.  $\frac{9}{64}$
    - C.  $\frac{8}{9}$
    - D.  $\frac{72}{64}$
- 10. What are the solutions of the equation  $3x^2 12 = 16x$ ?
  - A. x = 4, 1
  - B. x = -2, 2

C. 
$$x = \frac{2}{3}, -6$$

\* D. 
$$x = -\frac{2}{3}, 6$$

- **11.** Which expression is equivalent to  $2^{-3}$ ?
  - A. -8B.  $-\frac{1}{8}$ \* C.  $\frac{1}{8}$ D. 8
- 12. The object of a certain puzzle is to move rings off a post in the fewest number of steps. Moving the rings requires at least  $2^n - 1$  steps, where *n* is the number of rings on the post. If the post contains 7 rings, what is the **fewest** number of moves that can be made?
  - A. 13 moves
  - B. 64 moves
  - \* C. 127 moves
    - D. 128 moves

13. Which of the following is the graph of  $y = x^2 + 1$  after a reflection over the *x*-axis?



14. What value of *p* satisfies the equation 5p-3=8(p-1)+7p?

A. 
$$p = -\frac{2}{5}$$
  
B.  $p = -\frac{1}{5}$   
\* C.  $p = \frac{1}{2}$   
D.  $p = \frac{11}{10}$ 

**15.** A function is graphed below.



What are the coordinates of the minimum of this function?

- A. (-1,16)
- B. (0,7)
- C. (1, 0)
- \* D. (4, -9)

**16.** Which data set has a domain of 0, 1, 2, 4?

A.	x	у
	1	-3
	-1	4
	0	2
	-5	-8

C.	x	У
	_4	-3
	-2	-1
	-1	0
	0	1

- 17. Lee is painting a fence. If Lee can paint6 boards every 15 minutes, how many boardscan Lee paint in 3 hours?
  - A. 1.2
  - \* B. 72
    - C. 360
    - D. 450

x	У
-2	2
-1	1
0	0
-4	4

\* D.

B.

x	У
0	1
1	2
2	4
4	8

- 18. Consider the graph of y = 2x + b. If the constant, *b*, is decreased by 2, in which direction will the graph shift?
  - A. up
  - \* B. down
    - C. left
    - D. right

**19.** Look at the line segment graphed below.



What is the midpoint of the line segment?

A.	$\left(\frac{1}{2},1\right)$
B.	$\left(-\frac{3}{2},3\right)$
C.	(-1, -2)
* D.	$\left(-\frac{1}{2},-1\right)$

**20.** A system of equations is shown below.

$$2x + y = 7$$
$$3x - 2y = 0$$

What is the solution to this system?

\* A. (2, 3)

- B. (2, -3)
- C. (-7, 21)
- D. (7, -21)

**21.** Look at the graph below.



What is the slope of the line shown above?

\* A. 
$$-\frac{3}{5}$$
  
B.  $-\frac{5}{3}$   
C.  $-\frac{1}{3}$   
D.  $-3$ 

**22.** The graph below shows the population of deer over several years.



This graph best represents which of the following statements?

- A. The deer population remained stable over the years.
- B. Once a predator was removed, the deer population increased.
- C. Over the years the habitat area decreased, causing the deer population to decrease.
- \* D. An extremely cold winter killed off a large portion of the population. Afterward, the population recovered and stabilized.
- **23.** Look at the graph below.



Which inequality **best** describes the graph above?

- A. |x| < 4
- B.  $|x| \le 4$
- \* C. |x| > 4
- D.  $|x| \ge 4$

## PART II MID-YEAR RELEASED ALGEBRA I ITEMS

24. The matrices below show the number of T-shirts sold by day and by size and the price of each size.

Number of T-shirts sold			Price of	Price of T-shirts sold		
S	М	L	S	М	L	
Monday 12	15	22]	[\$6.00	\$8.00	\$10.00]	
Tuesday 14	24	18				

How much money was collected on Tuesday from medium (M) T-shirt sales?

A. \$120

- \* B. \$192
  - C. \$240
  - D. \$312

25. Why is  $\frac{(\sqrt{x} - \sqrt{11})^2}{x - 11}$  undefined when x = 11?

- A. The square root of 11 is undefined.
- B. The value of 0 squared is undefined.
- C. A fraction with a numerator of 0 is undefined.
- \* D. A fraction with a denominator of 0 is undefined.
- 26. Gaspar's Internet provider charges \$0.04 per minute each month for web service plus a monthly flat fee for a modem. If Gaspar paid \$67 last month and used 1,500 minutes of web service, how much does the modem cost per month?
  - A. \$ 1.17
  - B. \$ 2.68
  - \* C. \$ 7.00
  - D. \$60.00

27. A classroom has 30 chairs of various colors; 5 yellow, 10 red, 4 blue, and the rest green. The first student in the room sits in a green chair. If the second student coming into the room chooses a chair at random, what is the probability the chair will be green?

A. 
$$\frac{11}{30}$$
  
B.  $\frac{19}{30}$   
\* C.  $\frac{10}{29}$   
D.  $\frac{18}{29}$ 

- **28.** Which is the simplified form of the expression 10z 4 + 8(z 1)?
  - A. 6z B. 11z-12 C. 18z-5 \* D. 18z-12

- **29.** Before driving to her grandmother's house, Paula buys 10 gallons of gasoline for \$23.00. She drives 300 miles over 6 hours. At the end of each hour, she records how many miles she has driven. In a graph of her distance over time, what would be the dependent variable?
  - \* A. miles
    - B. hours
    - C. dollars
    - D. gallons
- **30.** Jan has a deck in the shape of a square. Jan extends each side of the deck by 6 feet. The area of the extended deck is 324 square feet. What was the side-length of the original deck in feet?



A. 6 \* B. 12 C. 18

D. 24

## PART II MID-YEAR RELEASED ALGEBRA I ITEMS

- A. Roger has a lawn care business and charges a flat fee of 20 dollars plus *x* dollars per hour to mow yards. It takes Roger 3 hours to mow one yard, 2 hours to mow a second yard, 1 hour to mow a third yard, and 4 hours to mow a fourth yard.
  - 1. Write four different expressions, each expression representing Roger's charge for one of the yards.
  - 2. Using the four different expressions from Part 1, write an expression that represents the sum of the charges for the four different yards. Show your work.
  - 3. If Roger earns \$175 mowing the four yards, how much does he charge per hour?

BE SURE TO LABEL YOUR RESPONSES 1, 2, AND 3.

#### Item A Scoring Rubric—2012 Algebra I

Score	Description
4	The student earns 4 points. The response contains no incorrect work. Label of "\$" is given with answer in Part 3
3	The student earns $3 - 3\frac{1}{2}$ points.
2	The student earns $2 - 2\frac{1}{2}$ points.
1	The student earns $\frac{1}{2} - \frac{1}{2}$ points, or some minimal understanding is shown.
0	The student earns 0 points. No understanding is shown.
В	Blank — No Response. A score of "B" will be reported as "NA." (No attempt to answer the item. Score of "0" is assigned for the item.)

## PART II MID-YEAR RELEASED ALGEBRA I ITEMS

**B.** The nutrition facts for three different brands of chocolate cookies are listed below.

<b>Nutrition Facts</b> Serving Size 2 cookies	<b>Nutrition Facts</b> Serving Size 2 cookies	<b>Nutrition Facts</b> Serving Size 2 cookies	
Amount Per Serving	Amount Per Serving	Amount Per Serving	
Calories130	Calories130	Calories160	
Calories from Fat50	Calories from Fat40	Calories from Fat63	
Total Fat6 g	Total Fat4.5 g	Total Fat7 g	
Sodium80 mg	Sodium 80 mg	Sodium190 mg	
Cookie #1	Cookie #2	Cookie #3	

A marketing company wants to create a matrix that will compare the calories, calories from fat, total fat, and the sodium per serving for the three brands of cookies.

- 1. Construct one matrix that includes the data from all three nutrition tables. Be sure to include all labels.
- 2. The marketing company decides to compare Cookie #2 with Cookie #3. The company wants a matrix that shows the differences in calories, calories from fat, total fat, and the sodium per serving. Construct a matrix that displays these data. Be sure to include all labels.
- 3. The marketing company decides to also compare Cookie #2 with Cookie #3 for the differences in calories, calories from fat, total fat, and the sodium per cookie. Construct a matrix that displays these data. Be sure to include all labels.

BE SURE TO LABEL YOUR RESPONSES 1, 2, AND 3.

Score	Description
4	The student earns 4 points. The response contains no incorrect work.
3	The student earns $3 - 3\frac{1}{2}$ points.
2	The student earns $2 - 2\frac{1}{2}$ points.
1	The student earns $\frac{1}{2} - \frac{1}{2}$ points, or some minimal understanding is shown.
0	The student earns 0 points. No understanding is shown.
В	Blank — No Response. A score of "B" will be reported as "NA." (No attempt to answer the item. Score of "0" is assigned for the item.)

#### Item B Scoring Rubric—2012 Algebra I

C. Copy the table below into your answer document.

x	У
-2	
-1	
0	
1	
2	

- 1. Complete the table in your answer document using values from the equation  $y = -x^2 + 1$ .
- 2. On the grid provided in your answer document, graph the function containing the points in the table.
- 3. What is the vertex of the function? Show your work or explain your answer.
- 4. If the function were reflected over the *x*-axis, what would be the coordinates of the new vertex? Show your work or explain your answer.

BE SURE TO LABEL YOUR RESPONSES 1, 2, 3, AND 4.

#### Item C Scoring Rubric—2012 Algebra I

Score	Description
4	The student earns 5 points. The response contains no incorrect work.
3	The student earns $3\frac{1}{2} - 4\frac{1}{2}$ points.
2	The student earns $2 - 3$ points.
1	The student earns $\frac{1}{2} - \frac{1}{2}$ points, or some minimal understanding is shown.
0	The student earns 0 points. No understanding is shown.
В	Blank — No Response. A score of "B" will be reported as "NA." (No attempt to answer the item. Score of "0" is assigned for the item.)

- 1. Nico puts \$250 into a savings account that earns 6% per year simple interest. How long will it take for Nico to earn \$90 interest?
  - A. 0.02 years
  - B. 0.17 years
  - \* C. 6 years
    - D. 46 years
- 2. A nursery records the weights of 6 newborn babies in pounds. The weights are shown below.
  - 7.7, 8.3, 7.5, 6.7, 9.0, 8.1

After the next baby is born, the mean weight of the 7 babies becomes 7.8 pounds. What is the weight of the seventh baby in pounds?

- \* A. 7.3
  - B. 7.8
  - C. 7.9
  - D. 8.1

- **3.** Lupe wants to survey a group of people to find out which three pop songs are the most popular. Which of the following groups would provide the **best** random sample?
  - A. her group of friends
  - B. the DJs at the local country radio station
  - \* C. every 10th person entering the shopping mall
    - D. the members of the town symphony orchestra
- 4. What are the solutions to the equation  $0 = 6x^2 + 13x 5?$

A. 
$$-\frac{5}{3} \text{ or } \frac{1}{2}$$
  
B.  $\frac{5}{6} \text{ or } -1$   
\* C.  $\frac{1}{3} \text{ or } -\frac{5}{2}$   
D.  $\frac{1}{3} \text{ or } \frac{5}{2}$ 

5. Elle babysits every month for a year and uses a scatterplot to show how much money she made. Which of the graphs below shows the line of best fit drawn correctly?



6. The verbal expression "the difference between three times a number *x* and 12, increased by the quotient of 5 and the number *x*" is equivalent to which algebraic expression?

A. 
$$3(x-12) + \frac{x}{5}$$

\* B. 
$$(3x-12) + \frac{5}{x}$$

C. 
$$3(x-12) + 5 + x$$

D. (3x-12)+5+x

7. Below is a list of coordinate pairs with the variable *x* listed in place of one of the domain values.

 $\{(2, 6), (x, 6), (5, 7), (6, 8), (8, 9)\}$ 

Which value of *x* will make the relation above a function?

\* A. 3

B. 5

- C. 6
- D. 8

8. Tim maps his neighborhood on a grid, as shown below.



If the fountain is located at the midpoint of the segment that connects Tim's house and the school, what are the coordinates of the fountain?

A. 
$$\left(-\frac{3}{2}, \frac{1}{2}\right)$$
  
B.  $\left(-2\frac{1}{2}, -1\right)$   
\* C.  $\left(-2\frac{1}{2}, \frac{1}{2}\right)$   
D.  $\left(-4, \frac{1}{2}\right)$ 

- 9. If f(x) = -4x + 2, what is f(-3)?
  - A. -10
  - В. —5
  - C. 12
  - \* D. 14
- 10. What is the expression equivalent to  $\frac{8}{\sqrt{3}}$ ?

A. 
$$8\frac{2}{3}$$

- B. 24
- C.  $8\sqrt{3}$
- \* D.  $\frac{8\sqrt{3}}{3}$

- 11. What are the factors of  $81x^2 + 36x + 4$ ?
  - A. (9x+2)(x+2)\* B. (9x+2)(9x+2)C. (9x-2)(9x-2)
    - D. (9x+2)(9x-2)
- 12. If 3b+12 = 5(b-4), what is b?
  - A. 4
  - B. 6
  - C. 8
  - \* D. 16

**13.** A travel club arranges bus trips for its members. The club charges \$20 to become a member and \$7 for each bus trip taken. Which graph represents the cost of taking bus trips with the club?



14. Which expression is equivalent to  $\sqrt{27} - \sqrt{12}$ ?

- A. 1 \* B.  $\sqrt{3}$ C.  $\sqrt{15}$ 
  - C.  $\sqrt{15}$ D.  $3\sqrt{3} - 2$

**15.** Terry and Todd each plot their weights from January to June on separate scatter plots shown below.



Which of the following is true based on these scatter plots?

- \* A. Todd is gaining weight at a faster rate than Terry is losing weight.
  - B. Terry is losing weight at the same rate that Todd is gaining weight.
  - C. Todd's weight is increasing while Terry's weight remains constant.
  - D. At these rates, Terry and Todd will be the same weight in December.

16. What are the solutions to the equation  $3x^2 + 11x - 4 = 0$ ?

A. x = -4, 1

B. 
$$x = 2, -2$$

C. 
$$x = \frac{2}{3}, -2$$

\* D.  $x = \frac{1}{3}, -4$ 

17. What is the value of the expression  $\sqrt{(x+y)^2 + (3z+2)}$  when x = 5, y = 6, and z = 7? A.  $\sqrt{34}$ B. 11 \* C. 12 D.  $2\sqrt{37}$ 

- **18.** Which is equivalent to  $(5^3)(5^9)$ ?
  - \* A. 5<sup>12</sup>
    - B. 5<sup>27</sup>
    - C. 10<sup>12</sup>
    - D. 25<sup>27</sup>
- 19. The function  $f(C) = \frac{9}{5}C + 32$  is used to convert the temperature from degrees Celsius to degrees Fahrenheit. If the temperature is currently  $-4^{\circ}$  Celsius, what is the temperature in degrees Fahrenheit?
  - A. −20° \* B. 24.8° C. 17.77° D. 50.4°

**20.** A toy rocket is launched from the ground. The graph below shows the height of the rocket over time, *x*.



At what time, *x*, does the rocket reach its maximum height?

- A. x = 0 seconds
- \* B. x = 2 seconds
  - C. x = 4 seconds
  - D. x = 20 seconds
- 21. An equation has been derived to estimate a person's maximum heart rate. Using that equation, the maximum heart rate of a 60-year-old is 160 beats per minute and the maximum heart rate of a 35-year-old is 185 beats per minute. If x represents age and yrepresents heart rate, which of the following could be the equation in point-slope form?

A. 
$$y - 35 = 25(x - 185)$$

B. 
$$y - 60 = 1(x - 185)$$

- \* C. y 160 = -1(x 60)
- D. y 35 = 25(x 160)

**22.** Look at the function table shown below.

x	У
-4	16
2	-8
4	-16
8	-32

What is the domain of the function?

- A. {2, 4, 8}
- \* B. {-4, 2, 4, 8}
  - C. {2, 4, 8, 16}
  - D.  $\{16, -8, -16, -32\}$
- 23. A ball is thrown straight up into the air with an initial velocity of 64 feet per second. The equation modeling the ball's motion is  $h = -16t^2 + 64t$  where *h* is the ball's height and *t* is time in seconds. What is the ball's height in feet after 3 seconds?
  - \* A. 48
    - B. 67
    - C. 144
    - D. 336

24. A store manager pays his sales associates \$29 for every shift worked. The manager also offers a bonus of \$1.50 for each item sold. The manager creates a graph that plots *x*, the number of items an employee sells, versus *y*, the amount of money each employee can earn per shift. What is the *y*-intercept for this graph?

A. 
$$(0, 1\frac{1}{2})$$
  
B.  $(0, 27\frac{1}{2})$   
C.  $(0, 29)$   
D.  $(0, 30\frac{1}{2})$ 

\*

- **25.** Which of the following shows causation with the statement, "Derek won the cross-country state championship."?
  - A. Derek trained every day.
  - \* B. Derek ran faster than the other racers.
    - C. Derek was in better shape than the other racers.
    - D. Derek was well rested the day of the state championship.
- 26. The function  $y = 2x^2$  is graphed on a coordinate plane. Which change in the function will result in a vertical shift up 3 units?

A. 
$$y = 5x^{2}$$
  
B.  $y = 6x^{2}$   
\* C.  $y = 2x^{2} + 3$   
D.  $y = 2x^{2} - 3$ 

### PART II SPRING RELEASED ALGEBRA I ITEMS

- 27. Which of the following is true of the lines given by the equations y = 4x - 4 and  $y = -\frac{1}{4}x + 4$ ?
  - A. They never intersect each other.
  - B. They are identical to each other.
  - C. They are parallel to each other.
  - \* D. They are perpendicular to each other.
- **28.** Which pattern of numbers can be produced by the formula  $a_n = 3n + 4$ ?
  - A. $\{3, 10, 17, 24\}$ B. $\{4, 8, 12, 16\}$ \* C. $\{7, 10, 13, 16\}$ D. $\{7, 11, 15, 19\}$

- **29.** If *x* and *y* vary directly, and y = -20 when x = 5, what is the value of *y* when x = 12?
  - A. −80 \* B. −48
    - C. 48
    - D. 80
- 30. Which expression is equivalent to  $\frac{x^2 4}{x + 2}$ , if  $x \neq -2$ ?
  - \* A. (x-2)B. (x+2)C. (x-6)
    - D.  $(x^3 2)$

## PART II SPRING RELEASED ALGEBRA I ITEMS

- A. A restaurant charges a reservation fee of \$15 for its party room, plus \$21.50 per person.
  - 1. Write an equation in slope-intercept form showing what the total cost, y, would be for a group of x number of people to hold a party there.
  - 2. On the grid in your answer document, graph the equation from Part 1.
  - 3. If the bill was \$445, how many people were at the party? Show your work or explain your answer.
  - 4. Describe how the graph from Part 2 would change if the reservation fee were raised to \$25.

BE SURE TO LABEL YOUR RESPONSES 1, 2, 3, AND 4.

#### Item A Scoring Rubric—2012 Algebra I

Score	Description
4	The student earns 4 points. The response contains no incorrect work. Graph is titled in Part 2.
3	The student earns $3 - 3\frac{1}{2}$ points.
2	The student earns $2 - 2\frac{1}{2}$ points.
1	The student earns $\frac{1}{2} - \frac{1}{2}$ points, or some minimal understanding is shown.
0	The student earns 0 points. No understanding is shown.
В	Blank — No Response. A score of "B" will be reported as "NA." (No attempt to answer the item. Score of "0" is assigned for the item.)

## PART II SPRING RELEASED ALGEBRA I ITEMS

- **B.** The formula  $s = \sqrt{30df}$  is used to find how fast a car was traveling before an accident, where s = speed (in mph), d = the length (in feet) of the skid mark left by the car, and f = the coefficient of friction (road condition). Sophie, a police officer, must decide if the driver in a car accident was speeding in a 35 mph speed zone. The car's skid-mark length (d) is 76 feet. The coefficient of friction (f) is 0.80.
  - 1. Write the equation Sophie needs to use, substituting in the values of d and f, to determine the speed of the car before the accident.
  - 2. Solve the equation in Part 1. Round your answer to the nearest tenth.
  - 3. Was the driver speeding in the 35 mph speed zone? Show your work and/or explain your answer.
  - 4. If the skid mark had been 4 times longer, how many times as fast would the driver have been going as compared to the speed found in Part 2? Show your work and/or explain your answer.

BE SURE TO LABEL YOUR RESPONSES 1, 2, 3, AND 4.

Item B Scoring Rubric—2012 Algebra I		
Score	Description	
4	The student earns 4 points. The response contains no incorrect work.	
3	The student earns $3 - 3\frac{1}{2}$ points.	
2	The student earns $2 - 2\frac{1}{2}$ points.	
1	The student earns $\frac{1}{2} - \frac{1}{2}$ points, or some minimal understanding is shown.	
0	The student earns 0 points. No understanding is shown.	
В	Blank — No Response. A score of "B" will be reported as "NA." (No attempt to answer the item. Score of "0" is assigned for the item.)	