DIRECTORATE FOR QUALITY AND STANDARDS IN EDUCATION
Department for Curriculum Management and eLearning Educational Assessment Unit
Annual Examinations for Secondary Schools 2011

FORM 4
MATHEMATICS SCHEME A
TIME: 20 minutes Non Calculator Paper

Name $\qquad$ Class $\qquad$

Mark

## Instructions to Candidates

- Answer all questions.
- This paper carries a total of 20 marks.
- Calculators and protractors are NOT ALLOWED.

| No. | QUESTION | Space for Working if Required |
| :---: | :---: | :---: |
| 1 | The locus of points which are a fixed distance from a point is: <br> (A) a perpendicular bisector <br> (B) a circle <br> (C) an angle bisector <br> (D) a regular octagon <br> Ans: $\qquad$ |  |
| 2 | A point $R(2,5)$ is translated by $\binom{-6}{3}$ to a point $S(a, b)$. Write down the values of $a$ and $b$. <br> Ans: $a=$ $\qquad$ ; $b=$ $\qquad$ |  |
| 3 | Write $2^{-3}$ as a fraction. <br> Ans: |  |
| 4 | Increase $€ 80$ by $25 \%$. <br> Ans: $€$ |  |
| 5 | Simplify: $\sqrt{\frac{100 p^{4}}{q^{2}}}$ <br> Ans: $\qquad$ |  |
| 6 | Express $1730 \mathrm{~mm}^{2}$ as $\mathrm{cm}^{2}$. <br> Ans: $\qquad$ $\mathrm{cm}^{2}$ |  |
| 7 | Work out $\left(2.7 \times 10^{9}\right) \times\left(3.0 \times 10^{-2}\right)$. Give your answer in standard form. <br> Ans: $\qquad$ |  |
| 8 | Write down the equation of the line which is parallel to $y=3 x-7$ and which cuts the $y$ axis at $(0,5)$. <br> Ans: $\qquad$ |  |


| 9 |  <br> What is the gradient of the line AB ? <br> Ans: |  |
| :---: | :---: | :---: |
| 10 | Expand and simplify: $(x+3)^{2}$ <br> Ans: |  |
| 11 | Factorise completely: $3 q r^{2}-27 q r$ <br> Ans: |  |
| 12 | Work out: $55^{2}-45^{2}$ <br> Ans: |  |
| 13 | Simplify: $\frac{1}{2 x}-\frac{1}{6 x}$ <br> Ans: $\qquad$ |  |
| 14 | Evaluate: $9^{6} \div 3^{10}$ <br> Ans: $\qquad$ |  |
| 15 | Make $y$ the subject of the formula $x=\sqrt{\frac{y}{2}}$. <br> Ans: $y=$ |  |
| 16 | $\mathrm{A}=7^{2} \times 5^{3} \times 3 \quad \mathrm{~B}=7^{4} \times 5 \times 2$ <br> What is the Highest Common Factor of A and B? <br> Ans: $\qquad$ |  |


| 17 | The area of the triangle is $120 \mathrm{~cm}^{2}$. Calculate the length of the base of this triangle. <br> Ans: $\qquad$ cm |  |
| :---: | :---: | :---: |
| 18 |  <br> Which of the following could be represented by this graph? <br> (A) The mass of a metal against its volume. <br> (B) The surface area of the floor against the number of tiles. <br> (C) The distance covered by a car against the volume of fuel left in the tank. <br> (D) Converting euro into US Dollars. <br> Ans: $\qquad$ |  |
| 19 | Points A, B and C lie on the circumference of a circle centre O . Calculate the reflex angle $\angle \mathrm{AOC}$. <br> Ans: $\qquad$ |  |
| 20 | The points on this wheel of radius 1 m are equally spaced. The wheel turns in the direction shown. Taking 3 as an estimate for $\pi$, work out the distance the wheel covers when point A touches the ground. <br> Ans: $\qquad$ m |  |

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FORM 4
MATHEMATICS SCHEME A
TIME: 1h 40min Main Paper

| Question | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | Total <br> Main | Non <br> Calculator | Global <br> Mark |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mark |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

DO NOT WRITE ABOVE THIS LINE

Name: $\qquad$ Class: $\qquad$

## CALCULATORS ARE ALLOWED BUT ALL NECESSARY WORKING MUST BE SHOWN. ANSWER ALL QUESTIONS.

1. Complete the following logo program which traces the shape shown. pd repeat $\qquad$ [fd 50 rt 90 fd $\qquad$ rt 90 fd 50 $\qquad$ 90]

2. The volume of a sphere is $288 \pi \mathrm{~cm}^{3}$. Calculate the radius of this sphere.

$$
\text { Volume of Sphere }=\frac{4}{3} \pi r^{3}
$$

Ans: $\qquad$ cm (3 Marks)
3. Solve the equation: $2 x^{2}+5 x-1=0$, giving your answers correct to $\mathbf{2}$ decimal places.

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

Ans: $x=$ $\qquad$ , $\qquad$
4.
a) Solve the equation: $\quad x=\frac{3(x-4)}{2}+\frac{x}{4}$

Ans: $x=$ $\qquad$
b) Solve the equation: $8+x(3 x+5)=3(1-x)$

Ans: $x=$ $\qquad$ , $\qquad$
c) Rearrange $4 a b=3 a k+1$ to make $\boldsymbol{a}$ the subject of the formula.

Ans: $a=$ $\qquad$
(9 Marks)
$\qquad$ Class $\qquad$
5. Gregory opened an account with Savers Bank on $1^{\text {st }}$ January 2008. He put $€ 2000$ into the account to start with. He then added an extra $€ 500$ at the end of each year. The bank pays compound interest at the rate of $4 \%$ per annum.
a) What was the amount on $1^{\text {st }}$ January 2010?

Ans: $€$ $\qquad$
b) What was the total interest on $1^{\text {st }}$ January 2010 ?

Ans: $€$ $\qquad$
6. The first part of a sequence is: $7,11,15,19, \ldots$
a) Find an expression for the $n^{\text {th }}$ term.
b) What is the $100^{\text {th }}$ term of the sequence?

Ans: $n^{\text {th }}$ term $=$ $\qquad$

Ans: $\qquad$
c) Which term of the sequence is 231 ?

Ans: $\qquad$
(6 Marks)
7. Kimberly looked at a passage from a book she was reading. She recorded the number of words in each sentence in the frequency table shown below.

| Number of words per sentence | Frequency $f$ | Mid-values $x$ | $f \times x$ |
| :---: | :---: | :---: | :---: |
| $1-5$ | 17 | 3 | 51 |
| $6-10$ | 27 |  |  |
| $11-15$ | 25 |  |  |
| $16-20$ | 15 |  |  |
| $21-25$ | 9 | 23 | 207 |
| $26-30$ | 4 |  |  |
| $31-35$ | 0 |  | 38 |
| $36-40$ | 1 |  | Total $=$ |
| $41-45$ | 2 |  |  |

a) Complete the table.
b) Write down the class interval in which the median number of words lies.

Ans: $\qquad$
c) Work out an estimate for the mean number of words per sentence.

Ans: $\qquad$
(7 Marks)
$\qquad$
8. A coin is biased. There is a $60 \%$ chance of getting Heads. You flip the coin three times.


Use the probability tree to calculate, as a percentage, the probability that:
a) you get three Heads.

Ans: $\qquad$ \%
b) you get one Head and two Tails.

Ans: $\qquad$ \%
c) you get at least one Tail.

Ans: $\qquad$ \%
(6 Marks)
9.


Points $\mathrm{B}, \mathrm{C}, \mathrm{D}$ and E lie on level ground. The angle of elevation of A from F is $12^{\circ}$. $\mathrm{BC}=2.2 \mathrm{~m}$ and $\mathrm{FD}=4.8 \mathrm{~m}$. Calculate the following distances correct to 2 decimal places.
a) FE

Ans: $\mathrm{FE}=$ $\qquad$ m
b) DE

Ans: $\mathrm{DE}=$ $\qquad$ m
c) AB

Ans: $\mathrm{AB}=$ m
d) BE

Ans: $\mathrm{BE}=$ $\qquad$ m
e) $C D$

Ans: $\mathrm{CD}=$ $\qquad$ m
10. Complete the proof to show that:
"The angle formed by a chord and a tangent at the point of contact is equal to the angle in the alternate segment".

To prove that: $\angle$ $\qquad$ $=\angle \mathrm{TSQ}$.

$\angle \mathrm{RQT}=90^{\circ}$ $\qquad$
(Write the reason on this line)

$$
\begin{align*}
& \angle \mathrm{QRT}+\angle \mathrm{RTQ}=\ldots \ldots(1) \quad \text { Angle sum of a triangle is } 180^{\circ} \\
& \angle \mathrm{PTQ}+\angle \mathrm{RTQ}=90^{\circ} \ldots \ldots . .(2) \quad \text { (Write the reason on this line) } \tag{2}
\end{align*}
$$

From (1) and (2)
$\angle \mathrm{QRT}+\angle \mathrm{RTQ}=\angle \mathrm{PTQ}+\angle \mathrm{RTQ}$

Therefore $\angle \mathrm{QRT}=\angle$ $\qquad$

Now $S$ is any point on the circumference.
$\angle \mathrm{TSQ}=\angle$ $\qquad$ Angles in the same segment are equal

Thus $\qquad$ $=\angle$ $\qquad$
11. $\mathrm{T}_{2}$ is the image of $\mathrm{T}_{1}$ after a $90^{\circ}$ clockwise rotation about a point P . Use ruler and compasses only to find point $P$ by construction. Label point $P$.

|  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

12. 

a) Complete the tables below for: $y=x^{2}-2 x-2$ and $y=\frac{4-4 x}{3}$

| $x$ | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x^{2}$ | 4 | 1 |  |  |  | 9 | 16 |
| $-2 x$ | 4 |  |  | -2 |  | -6 |  |
| -2 | -2 |  | -2 |  | -2 | -2 |  |
| $y$ | 6 |  |  |  |  | 1 |  |


| $x$ | -2 | 1 | 4 |
| :---: | :---: | :---: | :---: |
| $y$ |  | 0 |  |

b) Plot the graphs of $y=x^{2}-2 x-2$ and $y=\frac{4-4 x}{3}$ on the grid below.

c) Use your graphs to solve the simultaneous equations $y=x^{2}-2 x-2$ and
$y=\frac{4-4 x}{3}$. Give the answers correct to 1 decimal place.

Ans: $x=$ $\qquad$ , $y=$ $\qquad$ and $x=$ $\qquad$ , $y=$ $\qquad$
(8 Marks)
13.


The diagram shows a cross-section of a cylindrical water pipe of internal radius 5 cm . The water level is 2 cm at its deepest part as shown by the shaded segment.
a) Calculate, correct to 2 decimal places, the angle marked A .

Ans: $\mathrm{A}=$ $\qquad$
b) Calculate, correct to 2 decimal places, the area of the shaded segment.

Ans: $\qquad$ $\mathrm{cm}^{2}$
c) Water is flowing at $30 \mathrm{~cm} / \mathrm{s}$. Calculate the volume of water that passes through the pipe in one hour. Give the answer correct to the nearest litre.

Ans: $\qquad$ litres
(9 Marks)

