## Mathematics, Grade 10

## Session 1, Multiple-Choice Questions



1) The cone shown below has a radius of 8 feet and a height of 12 feet.


What is the volume of the cone?
A. $32 \pi$ cubic feet
B. $256 \pi$ cubic feet
C. $374 \pi$ cubic feet
D. $768 \pi$ cubic feet

## Reporting Category for Item 1: Measurement

2 Darlene went to the hardware store to purchase 581 feet of rope. The rope costs $\$ 0.61$ per yard. Which is closest to the amount of money Darlene needs to purchase the rope?
A. $\$ 100.00$
B. $\$ 120.00$
C. $\$ 360.00$
D. $\$ 1080.00$

3 The figure below shows a house with an attic, represented by $\triangle A B C$ with $A C=B C$. The distance from $A$ to $B$ is 42 feet. The slope (commonly referred to as the pitch) of the roof is $\frac{2}{3}$.


What is the height, $h$, of the attic?
A. 14 feet
B. 28 feet
C. 32 feet
D. 63 feet

Reporting Category for Item 3: Number Sense and Operations

## Mathematics, Grade 10

4 A company packages breakfast cereal in the two sizes of right cylindrical containers shown below. The containers are similar in shape.


How many cubic inches does the large container hold?
A. $90 \pi$ cubic inches
B. $135 \pi$ cubic inches
C. $360 \pi$ cubic inches
D. $540 \pi$ cubic inches

5 The graph below models the cost of manufacturing calculators.


Which equation shows the relationship between the number of calculators, $n$, and the total cost, $C$ ?
A. $C=300+n$
B. $C=300+0.08 n$
C. $C=300+12.5 n$
D. $C=300+15 n$

## Mathematics, Grade 10

6 Lani had a box that contained

- 1 blue marble;
- 1 green marble;
- 1 purple marble;
- 1 yellow marble; and
- 2 red marbles.

Lani removed one marble without looking, and she recorded the result. She placed the marble back in the box and repeated the procedure one more time. What is the probability that Lani removed a red marble followed by a blue marble?
A. $\frac{1}{36}$
B. $\frac{1}{18}$
C. $\frac{1}{3}$
D. $\frac{1}{2}$

## Reporting Category for Item 6: Data Analysis, Statistics, and Probability

7 What is the value of the expression $3|2-4|-7$ ?
A. -13
B. -1
C. 1
D. 13

8 Computers are designed around off/on switches that are used to represent numbers. In the following pattern, which represents the numbers from 0 to 10 , represents a switch that is on and represents a switch that is off.


Which of the following represents the number 11 ?
A.

B.

C.

D.


## Mathematics, Grade 10

9 A landscape artist is designing two triangular flowerbeds so that:

- $\triangle L I M \cong \triangle P B C$.
- $\triangle L I M$ encloses Flowerbed 1.
- $\triangle P B C$ encloses Flowerbed 2.
- The measure of $\angle C$ is $50^{\circ}$ and the measure of $\angle B$ is $75^{\circ}$.

Flowerbed 1


Flowerbed 2

What is the measure of $\angle L$ ?
A. $50^{\circ}$
B. $55^{\circ}$
C. $75^{\circ}$
D. $105^{\circ}$

Use the graph below to answer question 10.


10 Which of the following equations best represents the data in the graph?
A. $y=2 x+3$
B. $y=\frac{1}{2} x+3$
C. $y=2 x-3$
D. $y=\frac{1}{2} x-3$

## Mathematics, Grade 10

11 Which of the following equations does not represent a linear relationship?
A. $x y=12$
B. $x+y=12$
C. $y=12 x$
D. $x-y=12$

12 Solve the inequality $|x-7| \leq 8$ for $x$.
A. $0 \leq x \leq 15$
B. $-1 \leq x \leq 15$
C. $-1 \leq x \leq 16$
D. $-7 \leq x \leq 8$

## Mathematics, Grade 10

13 The number of bacteria in a culture doubles each hour. Which graph below best represents this situation?
A.

B.

C.

D.


## Mathematics, Grade 10

14 The heights of the 20 players on a school soccer team are recorded in the box-and-whisker plot shown below.


Based on the information given in the box-and-whisker plot, which of the following statements is true?
A. The mean height of the team is 69 inches.
B. Half the players' heights are between 67 and 72 inches.
C. The shortest player on the team is 67 inches.
D. The range of heights of players on the team is 5 inches.

Reporting Category for Item 14: Data Analysis, Statistics, and Probability

## Session 1, Short-Answer Questions



15 Solve the following equation for $x$.

$$
3 x-(2 x-3)=2 x+9
$$

## Reporting Category for Item 15: Patterns, Relations, and Algebra

16 Geoffrey is building a patio. The floor of his patio will be made of bricks. The diagram below shows the shape of each brick.

One Brick


Geoffrey can combine two bricks side-by-side to make different shapes. An example of one combination of two bricks is shown below.

Two Bricks


What combination of two bricks would have the smallest base perimeter?
Draw this combination in your Student Answer Booklet.

## Mathematics, Grade 10

## Session 1, Open-Response Question

17 Casey placed six identical cards in a box. Each card was marked with one integer using each of the integers $0,1,2,3,4$, and 5 once. Casey drew two cards at random, one at a time, without replacing the first card.
a. Make a list, chart, or diagram of the possible outcomes when choosing two cards in this manner.
b. What is the probability that the sum of the integers on the two cards is greater than 9 ?
c. Based on your response to part a., what is the most frequently occurring sum of the integers? What is the probability that this sum will occur?

## Session 1, Short-Answer Questions



18 What is the simplest form of the expression $\frac{2 x^{4} y^{2}}{x^{2} y^{2}}, x \neq 0, y \neq 0$ ?

Use the figure below to answer question 19.


19 Triangle $A B C$ is inscribed in a circle $O$. What is the measure of $\angle A$ ?

## Mathematics, Grade 10

## Session 1, Open-Response Questions

20 Theresa took a test that had a total of 50 questions. There were 20 openresponse questions and 30 short-answer questions on the test.
a. There was a total of 100 points on the test; each question on the test was worth the same number of points. How many points was each question worth? Show your work or explain how you obtained your answer.
b. Suppose that $90 \%$ was the minimum score required in order to earn an A on this test. How many questions could Theresa answer incorrectly and still earn an A? Show your work or explain how you obtained your answer.
c. If Theresa answered all of the short-answer questions correctly, what is the minimum percent of open-response questions that Theresa must answer correctly in order to receive a score of $90 \%$ on the test? Show your work or explain how you obtained your answer.

21 Alex wanted to find a pattern to predict the total number of diagonals in a convex polygon. He used each of the figures below to determine the number of diagonals in the 4 -sided convex polygon and the 5 -sided convex polygon shown below.



5-sided convex polygon
a. Create a table like the one shown below in your Student Answer Booklet. Complete the table to show the relationship between the number of sides, the number of diagonals drawn from each vertex, and the total number of diagonals in each of the convex polygons listed.

| Number of sides | 4 | 5 | 6 | 7 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Number of diagonals from each vertex | 1 | 2 | 3 |  |  |
| Total number of diagonals | 2 | 5 | 9 |  |  |

b. What is the total number of diagonals that a convex polygon of 12 sides has?
c. Write an expression which represents the number of diagonals that a convex polygon of $n$ sides has.

## Mathematics, Grade 10

## Session 2, Multiple-Choice Questions 國

22 The rectangle shown below has a width of 2.5 feet and a perimeter of 13 feet.


What is the area of the rectangle?
A. 4 square feet
B. 8 square feet
C. 10 square feet
D. 10.5 square feet

23 Isaac is going to draw $\Delta S T U$ on the grid shown below so that it is congruent to $\triangle P Q R$.


He located point $S$ at $(-1,0)$ and point $T$ at $(-4,4)$. Which of the following coordinates represents a possible location for point $U$ ?
A. $(-3,6)$
B. $(-3,7)$
C. $(-4,3)$
D. $(-4,7)$

## Mathematics, Grade 10

24 An important formula in statistics is $z=\frac{(x-\mu)}{\sigma}$. Which of the following represents this equation solved for $x$ in terms of $z, \mu$, and $\sigma$ ?
A. $x=z \sigma+\mu$
B. $x=z \sigma-\mu$
C. $x=\frac{z+\mu}{\sigma}$
D. $x=\frac{z-\mu}{\sigma}$

The circle graph below shows the Corbett family's monthly budget. The Corbett family has a total monthly income of $\$ 2,000$.

## Corbett Family's Monthly Budget



Mr. Corbett received a $\$ 100$ per month raise. He increased the transportation expense portion of the monthly budget by $\$ 100$. To the nearest percent, what portion of the Corbetts' income is now being spent on transportation expenses?
A. 14 percent
B. 19 percent
C. 20 percent
D. 21 percent

## Mathematics, Grade 10

26 A company that makes ballet shoes surveyed 200 customers. Each customer voted for one favorite color of ballet shoe. The bar graph shows the results.

Ballet Shoe Color Preferences (200 Total Votes)


Based on the data in the graph, which of the following is the best estimate of the number of customers who voted for "Pink"?
A. 80
B. 110
C. 140
D. 170

## Mathematics, Grade 10

27. If the graphs of $y=5 x+40$ and $y=10 x+20$ are drawn on the same axes, they will
A. not intersect.
B. intersect at $(5,10)$.
C. intersect at $(4,60)$.
D. intersect at $(12,100)$.

Reporting Category for Item 27: Patterns, Relations, and Algebra
28 Let $x$ and $y$ be real numbers with $x<y<1$. Which of the following is always a real number that lies between $x$ and $y$ ?
A. $x-y$
B. $x+y$
C. $\frac{x-y}{2}$
D. $\frac{x+y}{2}$

## Mathematics, Grade 10

29 The average life spans of some animals are shown in the chart below.

Animal Life Spans

| Animal | Average Life Span (in years) |
| :---: | :---: |
| Bear | 22 |
| Chicken | 7 |
| Deer | 12 |
| Dog | 11 |
| Duck | 10 |
| Elephant | 35 |
| Fox | 9 |
| Horse | 22 |
| Hippopotamus | 30 |
| Wolf | 11 |

Source: Farmer's Almanac 2000.
Based on the information given in the chart, which of the following statistics yields the greatest numerical value?
A. mean
B. median
C. mode
D. range

30 Janet is playing a game using the two spinners shown below. She will spin the arrow on each spinner once and will move a specified number of steps forward or backward according to the results of the spins.


Spinner 1


Spinner 2

What is the probability that Janet will have to move backward less than 4 steps?
A. $\frac{1}{8}$
B. $\frac{3}{8}$
C. $\frac{1}{2}$
D. $\frac{3}{4}$

## Mathematics, Grade 10

## Session 2, Open-Response Question

31 When a diver goes underwater, the weight of the water exerts pressure on the diver. The table below shows how the water pressure on the diver increases as the diver's depth increases.

Water Pressure on a Diver

| Diver's Depth <br> (in feet) | Water Pressure <br> (in pounds per square inch) |
| :---: | :---: |
| 10 | 4.4 |
| 20 | 8.8 |
| 30 | 13.2 |
| 40 | 17.6 |
| 50 | 22.0 |

a. Based on the table above, what will be the water pressure on a diver at a depth of 60 feet? Show your work or explain how you obtained your answer.
b. Based on the table above, what will be the water pressure on a diver at a depth of 100 feet? Show your work or explain how you obtained your answer.
c. Write an equation that describes the relationship between the depth, $D$, and the pressure, $P$, based on the pattern shown in the table.
d. Use your equation from part c to determine the depth of the diver, assuming the water pressure on the diver is 46.2 pounds per square inch. Show your work or explain how you obtained your answer.

## Session 2, Multiple-Choice Questions

In her closet, Megan has 6 different T-shirts, 5 different pairs of shorts, and 2 different hats. She pulls out 1 T-shirt, 1 pair of shorts, and 1 hat without looking. How many different combinations of 1 T-shirt, 1 pair of shorts, and 1 hat are possible?
A. 11
B. 16
C. 32
D. 60

## Reporting Category for Item 32: Data Analysis, Statistics, and Probability

33 The can of corn shown below is a right circular cylinder with a height of 11 cm . The volume of the can is 486 cubic centimeters.


What is the approximate radius of the can of corn?
A. 1.3 cm
B. 3.8 cm
C. 7.0 cm
D. 14.1 cm

## Mathematics, Grade 10

34 The bar graph below shows the distribution of scores on a biology test.


Test Score Range

Based on the graph, which of the following is not a valid conclusion?
A. The total number of students tested was 27.
B. At least 5 students scored fewer than 60 points.
C. A total of 9 students scored 75 points or fewer.
D. At least 8 students scored more than 80 points.

## Mathematics, Grade 10

35 The lengths of three sides of a triangle are 5, 9, and $x$, all measured in centimeters. What are all possible values of $x$ ?
A. $4<x<14$
B. $0<x<14$
C. $5<x<15$
D. $3<x<9$

36 A set contains the numbers
$\frac{8}{2},-2.3,0, \frac{2}{7}, \sqrt{9}, 0 . \overline{31}, \sqrt{15},-12,2 \pi$.
Which of the following statements is true?
A. The set contains 8 irrational numbers.
B. The set contains 7 irrational numbers.
C. The set contains 3 irrational numbers.
D. The set contains 2 irrational numbers.

## Mathematics, Grade 10

37 Aircraft design engineers use the formula $V=\sqrt{\frac{841 L}{C S}}$ to determine the safe landing speed of aircraft where
$V=$ safe landing speed in feet per second
$L=$ gross weight of the aircraft in pounds
$C=$ coefficient of lift
$S=$ wing surface area in square feet.
What is the approximate safe landing speed for an aircraft with a gross weight of 9000 pounds and a wing surface area of 225 square feet, when the coefficient of lift is 2.8 ?
A. 4 feet per second
B. 110 feet per second
C. 414 feet per second
D. 22,000 feet per second

## Reporting Category for Item 37: Number Sense and Operations

38 On January 1, 2000, a car had a value of $\$ 15,000$. Each year after that, the car's value will decrease by 20 percent of the previous year's value. Which expression represents the car's value on January 1, 2003?
A. $15,000(0.8)^{3}$
B. $15,000(0.8)^{4}$
C. $15,000(0.2)^{3}$
D. $15,000(0.2)^{4}$

## Mathematics, Grade 10

39 Which of the following equations represents a line that is parallel to the line $4 x-2 y=8$ and passes through the point $(0,-8) ?$
A. $2 x+y=-4$
B. $2 x-y=8$
C. $x-2 y=8$
D. $x-2 y=16$
(40) What is the effect on the circumference of a circle if the circle's radius is doubled?
A. The circumference is multiplied by 2 .
B. The circumference is multiplied by 4 .
C. The circumference is multiplied by 8 .
D. The circumference stays the same.

## Mathematics, Grade 10

## Session 2, Open-Response Questions

41 Cube $A$ is a 1-inch solid cube. Figure $B$ shows a 1-inch solid cube after a cylindrical hole has been drilled through its center. The diameter of the cylindrical hole is $\frac{1}{2}$ inch, and its height is perpendicular to two opposite faces of the original cube, as shown in the diagram.

a. What is the total surface area of Cube A?
b. What is the total surface area of Figure B? Show your work or explain how you obtained your answer.

## Mathematics, Grade 10

42 The diagram shown below represents the path of a ball that is dropped from a height of 18 feet. On its first bounce, the ball rebounds to a height of 12 feet; on its second bounce, it rebounds to a height of 8 feet.

a. Show that the ratio of the height of Bounce 1 to the starting height is equal to the ratio of the height of Bounce 2 to the height of Bounce 1 . Show your work or explain how you obtained your answer.
b. Create a table like the one shown below in your Student Answer Booklet.

| Bounce, $\boldsymbol{b}$ | Height, $\boldsymbol{h}$ <br> (in feet) |
| :---: | :---: |
| 0 (Starting height) | 18 |
| 1 | 12 |
| 2 | 8 |
| 3 |  |
| 4 |  |
| 5 |  |

If the pattern in the table continues, complete your table to show the height of bounces 3,4 , and 5 .
c. Based on the pattern shown in the table, if $h$ is the height of a certain bounce, write an expression that represents the height of the next bounce in terms of $h$.
d. Based on the pattern shown in the table, write an equation that represents the relationship between height, $h$, and bounce, $b$.

