## Grade 8

Form R

## North Carolina

## End-of-Grade Tests-Grade 8

## Mathematics-Calculator Active

## Public Schools of North Carolina

 www.ncpublicschools.orgState Board of Education
Department of Public Instruction
Division of Accountability Services/North Carolina Testing Program Raleigh, North Carolina 27699-6314


1. Which is the largest value?

A $6 \sqrt{2}$

B $4 \sqrt{3}$

C $3 \sqrt{5}$
D $2 \sqrt{10}$
2. What is the approximate length of the diagonal of a square if the perimeter of the square is 12 ft ?

A $\quad 1.7 \mathrm{ft}$
B $\quad 3.5 \mathrm{ft}$
C $\quad 4.2 \mathrm{ft}$
D $\quad 12.7 \mathrm{ft}$
3. Which set of real numbers contains only rational numbers?

A $\quad\{\sqrt{121}, \sqrt{196}, \sqrt{24}, 12\}$

В $\quad\left\{\sqrt{144}, \frac{13}{2}, \frac{5}{3}, \sqrt{10}\right\}$

C $\quad\left\{\sqrt{169}, \frac{5}{2}, \sqrt{121}, \frac{14}{4}\right\}$

D $\quad\left\{\sqrt{169}, \frac{58}{3}, \frac{13}{2}, \sqrt{31}\right\}$
4. A 70-foot tree has a 35 -foot shadow. If the building next to the tree has an 80 -foot shadow, how tall is the building?

A 160 feet
B 120 feet

C 115 feet
D 40 feet
5. Ralph's garden is in the shape of a square. How does the area of the garden change if he doubles the length of each side of the garden?

A The area is halved.
B The area is doubled.
C The area is tripled.
D The area is quadrupled.
6. Constance bought a box to hold her jelly beans. The dimensions of the box are 6 inches by 2 inches by 1 inch. The jelly beans weigh a total of 36 ounces. If each cubic inch inside the box can hold two ounces, how many ounces of jelly beans will have to be left out of the box?

A 24
B 18
C 12
D 6
7. In the figure shown below, $\Delta A^{\prime} B^{\prime} C^{\prime}$ is the image produced by applying a dilation to $\triangle A B C$.


What is the scale factor for this dilation?
A $\quad \frac{1}{3}$

B $\frac{2}{5}$

C $\quad \frac{1}{2}$

D $\frac{5}{2}$
8. Which scatterplot shows a positive correlation between the variables?
A

B

C

D

9. The direct route from Marta's apartment to work is a road that is a straight line. The road is closed for repairs. Marta had to drive 8 miles west and then 6 miles south to get to work. She returned home by the same route. How many miles would she have saved round-trip if she had taken the direct route?

A 2
B 8
C 10
D 24
10. Harold took a survey on America's favorite movies by asking 50 students at his school to complete the survey. Which is the best reason why his survey may be flawed?

A The students were not old enough to take a survey.

B Some students are not American citizens.

C The students may include people who do not go to the movies.

D Harold is not getting a diverse representation from the American population.
11. The data displayed represent what type of correlation?


A a positive correlation where the $y$ values are exactly predicted by the line of best fit
B a negative correlation where the $y$ values are exactly predicted by the line of best fit
C a positive correlation where the $y$ values are approximately predicted by the line of best fit

D a negative correlation where the $y$ values are approximately predicted by the line of best fit
12. The Smiths made a scatterplot comparing their daily electricity costs to the outside temperature.


If the high temperature on a day is $95^{\circ}$, about how much will their cost for electricity be on that day?

A $\$ 0.95$
B $\quad \$ 0.70$
C $\quad \$ 0.67$
D $\quad \$ 0.64$
13. Which data will most likely show a negative correlation when graphed on a scatterplot?

A the outside temperature and the number of people wearing gloves

B the distance a student lives from school and the amount of time it takes to get to school

C the number of visitors at an amusement park and the length of the lines for the rides

D a student's height and grade point average
14. Hector's math test grades for the final quarter are $89,93,100,98$, and 95. He has one more test to take this quarter. All tests count equally. What is the minimum grade Hector must make on the last test in order to obtain an average of at least 93 ?

A 78
B 79
C 83
D 95
15. Solve for $b$ :

$$
3 b^{3}=81
$$

A 9
B 6.2
C 3
D 1.4
16. Which statement best describes the similarities of the graphs $2 y=5 x+\frac{6}{7}$ and $2 y=3 x+\frac{6}{7}$ ?

A The $y$-intercepts are the same.
B The slopes are the same.
C The $x$-intercepts are the same.
D The graphs are identical.
17. What is the slope of the line graphed below?


A $\quad{ }^{-} 2$
B $\quad-\frac{1}{2}$

C 1
D 2
18. The equation for a balanced seesaw is $w_{1} d_{1}=w_{2} d_{2}$. As shown in the figure below, $w_{1}$ and $w_{2}$ are weights, and $d_{2}$ and $d_{1}$ are distances from the balance point.


If $w_{1}=50$ pounds, $d_{1}=5$ feet, and $w_{2}=100$ pounds, what value of $d_{2}$ would balance the seesaw?

A 2.5 feet
B $\quad 5.0$ feet
C $\quad 7.5$ feet
D 10.0 feet
19. A line has a slope of $\frac{-2}{3}$ and a $y$-intercept of ${ }^{-} 10$. Which is an equation of the line?

A $2 x-3 y=-30$
B $\quad 2 x-3 y=-10$
C $\quad 2 x+3 y=10$
D $2 x+3 y={ }^{-} 30$
20. Which is the correct graph for $3 y=2 x-3$ ?
A

B

C

D

21. Mary's fish tank can hold $11 \sqrt{2}$ gallons of water. Which is the greatest number of gallons of water it can hold without overflowing?

A 22
B 15
C $\quad 9$
D 5
22. Which choice lists the lengths in order from least to greatest?

A $\quad \frac{1}{3} \mathrm{ft}, 0.25 \mathrm{ft}, 2 \mathrm{ft}, \sqrt{8} \mathrm{ft}$

B $\quad 0.25 \mathrm{ft}, \frac{1}{3} \mathrm{ft}, \sqrt{8} \mathrm{ft}, 2 \mathrm{ft}$

C $\quad 0.25 \mathrm{ft}, \frac{1}{3} \mathrm{ft}, 2 \mathrm{ft}, \sqrt{8} \mathrm{ft}$

D $\quad 2 \mathrm{ft}, 0.25 \mathrm{ft}, \frac{1}{3} \mathrm{ft}, \sqrt{8} \mathrm{ft}$
23. The two legs of a right triangle have lengths 5 and 7. Which term best describes the length of the hypotenuse?

A an irrational number less than 9
B an irrational number greater than 9

C a rational number less than 9
D a rational number greater than 9
24. If three is added to both the length and width of the rectangle, what will happen to the area?

5 in.

2 in.


A The area will be four times the original area.

B The area will be three times the original area.

C The area will be 12 sq in. more than the original area.

D The area will be 4 sq in. more than the original area.
25. Joe wanted to know the distance across a river. He made a drawing with two similar triangles, as shown below.

6.4 cm
5.0 m


What is the distance across the river, $x$ ?

A $\quad 1.6 \mathrm{~m}$
B $\quad 9.4 \mathrm{~m}$
C $\quad 16.0 \mathrm{~m}$
D $\quad 25.6 \mathrm{~m}$
26. A square tile has an area of 110 square centimeters. Which is the best estimate of the length of one side?

A 10.0 centimeters
B 10.5 centimeters
C 11.0 centimeters
D 11.5 centimeters
27. The vertices of a rectangle are $(0,0),(0,4),(2,4),(2,0)$. Which of the following points is a vertex for the image produced by a dilation with a scale factor of $\frac{1}{2}$ ?

A $(0,3)$

B $(0,2)$
C $(0,1)$
D $(2,1)$
28. Kendra has a rectangular poster board with dimensions of 10 ft by 4 ft . She would like to cut this poster board into 6 pieces, so she can construct a box.


If she uses the indicated cutting guides, what will be the dimensions of her box?

A $\quad 2 \mathrm{ft} \times 2 \mathrm{ft} \times 4 \mathrm{ft}$
B $\quad 4 \mathrm{ft} \times 4 \mathrm{ft} \times 2 \mathrm{ft}$
C $\quad 5 \mathrm{ft} \times 2 \mathrm{ft} \times 1 \mathrm{ft}$
D $\quad 10 \mathrm{ft} \times 4 \mathrm{ft} \times 1 \mathrm{ft}$
29. Which scatterplot displays a negative correlation?
A

19851990199520002005


B

D

30. Which suggestion would result in an unbiased sample that would best represent the favorite books of the whole eighth-grade class?

A Ask five randomly chosen students from each class in the eighth grade.

B Ask eighth-grade girls.
C Ask randomly chosen eighth-grade students who play sports.

D Ask students in the library after school.
31. This scatterplot could show the relationship between which two variables?


A speed of an airplane ( $x$ ) vs. distance traveled in one hour $(y)$

B outside air temperature ( $x$ ) vs. air conditioning costs $(y)$

C age of an adult ( $x$ ) vs. height of an adult ( $y$ )

D distance traveled ( $x$ ) vs. gas remaining in the tank $(y)$
32. According to the pattern established in the scatterplot, what $y$-value would correspond to an $x$-value of 11 ?


A 32
B 25
C 15
D 8
33. Bill collected and plotted data concerning gestation and longevity for a science project.

Animal Gestation vs. Longevity


Based on the line of best fit shown, about how long would an animal be expected to live if its gestation period is 300 days?

A 10 years
B 12 years
C 20 years
D 22 years
34. A rental company charges a flat fee of $\$ 50$ to rent a jet ski. In addition, renters must pay $\$ 17.50$ per hour of ski use. Which equation correctly represents the total cost, $c$, to rent a jet ski for $h$ hours?

A $\quad c=50.00 h+17.50$
B $\quad c=17.50 h+50.00$
C $\quad c=32.5 h$
D $c=67.5 h$
35. Heather recorded the 7 a.m. temperature at her house the first five days of four different months. Which data are nonlinear?
A
January

| Day | ${ }^{\circ} \mathbf{F}$ |
| :---: | :---: |
| 1 | ${ }^{-} 1$ |
| 2 | 4 |
| 3 | 9 |
| 4 | 14 |
| 5 | 19 |

B | February |  |
| :---: | :---: |
| Day | ${ }^{\circ} \mathbf{F}$ |
| 1 | 31 |
| 2 | 29 |
| 3 | 27 |
| 4 | 25 |
| 5 | 23 |

C

| March |  |
| :---: | :---: |
| Day | ${ }^{\circ} \mathbf{F}$ |
| 1 | 41 |
| 2 | 51 |
| 3 | 46 |
| 4 | 51 |
| 5 | 53 |

D

| Day | ${ }^{\circ} \mathbf{F}$ |
| :---: | :---: |
| 1 | 53 |
| 2 | 57 |
| 3 | 61 |
| 4 | 65 |
| 5 | 69 |

36. 

Which line has a slope of $\frac{1}{2}$ and passes through the point $(2,3) ?$

A


C


B


D

37. What is the equation of the line that contains the point $\left(\frac{1}{2},-3\right)$ and has a slope of -3 ?

A $y=-3 x-\frac{3}{2}$

B $y=-3 x-\frac{17}{2}$

C $\quad y=-3 x+\frac{3}{2}$

D $y={ }^{-} 3 x+\frac{17}{2}$
38. A cube has a volume of 24 cubic units. What is the approximate length of each side of the cube?

A 8 units
B 4.9 units
C 2.9 units
D 2 units
39. The equation $y=\frac{9}{5} x+32$ can be used to find Fahrenheit temperature ( $y$ ) when given Celsius temperature $(x)$. If this equation were graphed in a coordinate plane, what would be the $x$ - and $y$-intercepts?

A $\quad x$-intercept $=(32,0) ; y$-intercept $=\left(0, \frac{-160}{9}\right)$

B $\quad x$-intercept $=(0,32) ; y$-intercept $=\left(-\frac{160}{9}, 0\right)$

C $\quad x$-intercept $=\left(0, \frac{-160}{9}\right) ; y$-intercept $=(32,0)$

D $\quad x$-intercept $=\left(-\frac{160}{9}, 0\right) ; y$-intercept $=(0,32)$
40. A truck rental company charges $\$ 20$ plus 9 cents per mile. Joe's friend offers to rent Joe his truck for $\$ 35$ and won't charge him mileage. What is the minimum number of miles Joe has to drive to save money using his friend's truck?

A $\quad 17$
B 55
C 121
D 167
41. What is the order of the numbers from least to greatest?

$$
\sqrt{2}, \sqrt[3]{16}, \frac{15}{7}, 1.6
$$

A $1.6, \sqrt{2}, \sqrt[3]{16}, \frac{15}{7}$

В $\quad \sqrt{2}, 1.6, \frac{15}{7}, \sqrt[3]{16}$

C $\quad 1.6, \sqrt{2}, \frac{15}{7}, \sqrt[3]{16}$

D $\quad \sqrt{2}, \sqrt[3]{16}, \frac{15}{7}, 1.6$
42. The formula $s=20 \sqrt{273+T}$ gives an estimate for the speed $(s)$ of sound in meters per second when the air temperature is $T^{\circ} \mathrm{C}$. About how fast is the speed of sound when the temperature is ${ }^{-} 5^{\circ} \mathrm{C}$ ?

A $\quad 268 \mathrm{~m} / \mathrm{s}$
B $\quad 278 \mathrm{~m} / \mathrm{s}$
C $\quad 327 \mathrm{~m} / \mathrm{s}$
D $\quad 333 \mathrm{~m} / \mathrm{s}$
43. The solution to an inequality is $x \geq 5$. Which number is included in that solution?

A $\sqrt{10}$
B $\sqrt{30}$
C $2 \sqrt{5}$
D $3 \sqrt{2}$
44. What is the perimeter of a triangle whose dimensions are three times the size of $\triangle P Q R$ ?


A 23 ft
B $\quad 27.1 \mathrm{ft}$
C $\quad 69 \mathrm{ft}$
D $\quad 81.3 \mathrm{ft}$
45. A tree has a shadow 12 feet long. At the same time, John, who is five feet tall, has a shadow 4 feet long. If Sherry wants to find the height of the tree, which proportion should she use?

A $\quad \frac{x}{4}=\frac{5}{12}$

B $\quad \frac{x}{5}=\frac{8}{4}$

C $\quad \frac{x}{8}=\frac{5}{4}$

D $\quad \frac{x}{12}=\frac{5}{4}$
46. Triangle $A B C$ has vertices at $A(2,2)$, $B(2,7)$, and $C(6,3)$. This triangle is dilated by a scale factor of 3 . What is the location of point $C^{\prime}$ ?

A $(2,1)$
B $(6,6)$
C $(6,21)$
D $(18,9)$
47. The diagonal of a square television screen measures 27 inches. What is the approximate length of the screen?

A 13 in.
B 15 in .
C 19 in.
D $\quad 21 \mathrm{in}$.
48. The coffee can below is $\frac{3}{4}$ full.


How much coffee is in the can?

A about 57 in. ${ }^{3}$
B about 130 in. ${ }^{3}$
C about $170 \mathrm{in}^{3}{ }^{3}$
D about 226 in. ${ }^{3}$
49. Each point on the graph represents the relationship between the number of pencils in a package and how much the package costs.


Which package has the highest cost for each pencil?

A $W$
B $X$
C $Y$
D $Z$
50. Charles researched the price of video games over the last decade.

Video Game Prices


Based on the data shown, what would be the projected price of a video game in $2005 ?$
A $\quad \$ 9.50$
B $\quad \$ 15.50$
C $\quad \$ 18.00$
D $\quad \$ 19.50$
51. Mr. Larson's first math test resulted in the following grades:

$$
\begin{aligned}
& 21,23,35,43,46,50,53,59, \\
& 62,66,66,66,67,75,89,95
\end{aligned}
$$

A passing grade is anything above a 60. Mr. Larson says the central tendency for the class was to fail the test. Which statistical measure supports his claim?

A mode
B median
C upper quartile
D mean
52. Kevin made a scatterplot of noon temperatures for a two-week period.

Noon Temperatures


Which statement about the data is most accurate?

A The temperature had a slight increase each day.
B The temperature had a slight decrease each day.
C There was a trend for the temperature to increase during the second week.
D There was a trend for the temperature to increase during the first week.
53. A scatterplot is shown to have a negative relationship between the two variables. Which line of best fit could represent that scatterplot?

A $y={ }^{-} 2 x+4$

B $\quad y={ }^{-} 1$

C $\quad y=x-5$

D $\quad y=3 x+4$
54. Which would be an appropriate first step to solve $y=5 x+3$ for $x$ ?

A subtract 3 from both sides
B add 3 to both sides
C subtract 5 from both sides
D add 5 to both sides
55. Brittany programs the treadmill so that she will burn 3.2 calories per minute as she works out. What is the equation relating walking time $(x)$ in minutes to total calories burned $(y)$ ?

A $y=3.2 x$

B $y=3.2+x$

C $y=\frac{3.2}{x}$

D $\quad y=\frac{x}{3.2}$
56. The cost of attending the state fair is a $\$ 5.00$ admission charge and $\$ 1.50$ per ride. Elizabeth's mother gave her $d$ dollars to spend at the state fair. Which equation could be used to determine the maximum number of rides, $r$, Elizabeth can go on?

A $\quad r=1.50 d+5.00$
B $\quad r=(d+5.00) \div 1.50$
C $\quad r=(d-5.00) \div 1.50$
D $\quad r=1.50 d-5.00$
57. The equation $d=65 h$ describes the distance ( $d$ ) a vehicle travels in $h$ hours. Based on this formula, how long will it take a car to travel

90 miles?
A 98 minutes
B $\quad 83$ minutes
C 43 minutes
D 25 minutes
58. Which equation is nonlinear?

A $\quad 2 x-y=9$
B $\quad y=x^{2}+3$
C $y=2 x-3$
D $\quad x=y$
59. What is the slope of the line that passes through the points $(1,-3)$ and $(4,2) ?$

A $\quad \frac{5}{3}$

B $\frac{3}{5}$

C $-\frac{3}{5}$

D $\quad-\frac{5}{3}$
60. What is the equation of the line with a slope of $\frac{2}{3}$ and a $y$-intercept of 4 ?

A $2 x+3 y=12$
B $\quad 2 x+3 y=4$

C $\quad 3 x-2 y=-4$

D $2 x-3 y={ }^{-} 12$


End of MathematicsCalculator Active

# North Carolina Test of Mathematics <br> Grade 8 Form R RELEASED Fall 2009 <br> Answer Key 

## CALCULATOR ACTIVE



| Item Number | Correct Answer | Goal |
| :---: | :---: | :---: |
| 1 | A | 1 - Number and Operations |
| 2 | C | 1 - Number and Operations |
| 3 | C | 1 - Number and Operations |
| 4 | A | 2-Measurement |
| 5 | D | 2 - Measurement |
| 6 | C | 3 - Geometry |
| 7 | C | 3 - Geometry |
| 8 | A | 4 - Data Analysis and Probability |
| 9 | B | 3 - Geometry |
| 10 | D | 4 - Data Analysis and Probability |
| 11 | C | 4 - Data Analysis and Probability |
| 12 | C | 4 - Data Analysis and Probability |
| 13 | A | 4 - Data Analysis and Probability |
| 14 | C | 5 - Algebra |
| 15 | C | 5 - Algebra |
| 16 | A | 5 - Algebra |
| 17 | D | 5 - Algebra |
| 18 | A | 5 - Algebra |
| 19 | D | 5 - Algebra |
| 20 | B | 5 - Algebra |
| 21 | B | 1 - Number and Operations |
| 22 | C | 1 - Number and Operations |
| 23 | A | 1 - Number and Operations |
| 24 | A | 2-Measurement |
| 25 | C | 2 - Measurement |
| 26 | B | 3 - Geometry |
| 27 | B | 3 - Geometry |
| 28 | A | 3 - Geometry |
| 29 | B | 4 - Data Analysis and Probability |
| 30 | A | 4 - Data Analysis and Probability |
| 31 | D | 4 - Data Analysis and Probability |
| 32 | D | 4 - Data Analysis and Probability |
| 33 | C | 4 - Data Analysis and Probability |
| 34 | B | 5 - Algebra |
| 35 | C | 5 - Algebra |
| 36 | B | 5 - Algebra |
| 37 | A | 5 - Algebra |
| 38 | C | 5 - Algebra |
| 39 | D | 5 - Algebra |

# North Carolina Test of Mathematics <br> Grade 8 Form R RELEASED Fall 2009 <br> Answer Key 

| 40 | D | 5 - Algebra |
| :--- | :--- | :--- |
| 41 | B | 1 - Number and Operations |
| 42 | C | 1 - Number and Operations |
| 43 | B | 1 - Number and Operations |
| 44 | C | $2-$ Measurement |
| 45 | D | $2-$ Measurement |
| 46 | D | $3-$ Geometry |
| 47 | C | $3-$ Geometry |
| 48 | C | $3-$ Geometry |
| 49 | A | $4-$ Data Analysis and Probability |
| 50 | B | $4-$ Data Analysis and Probability |
| 51 | D | $4-$ Data Analysis and Probability |
| 52 | D | $4-$ Data Analysis and Probability |
| 53 | A | $4-$ Data Analysis and Probability |
| 54 | A | $5-$ Algebra |
| 55 | A | $5-$ Algebra |
| 56 | C | $5-$ Algebra |
| 57 | B | $5-$ Algebra |
| 58 | B | $5-$ Algebra |
| 59 | A | $5-$ Algebra |
| 60 | D | 5 - Algebra |

