

TRENDS IN INTERNATIONAL MATHEMATICS AND SCIENCE STUDY

TIMSS



TIMSS & PIRLS
International Study Center
Lynch School of Education, Boston College



TIMSS 2011 User Guide
for the International Database

Released Items

Mathematics – Eighth Grade

Which of these is the BEST estimate of $\frac{7.21 \times 3.86}{10.09}$?

(A) $\frac{7 \times 3}{10}$

(B) $\frac{7 \times 4}{10}$

(C) $\frac{7 \times 3}{11}$

(D) $\frac{7 \times 4}{11}$

M032166

Content Domain

Number

Topic Area

Fractions and Decimals

Cognitive Domain

Knowing

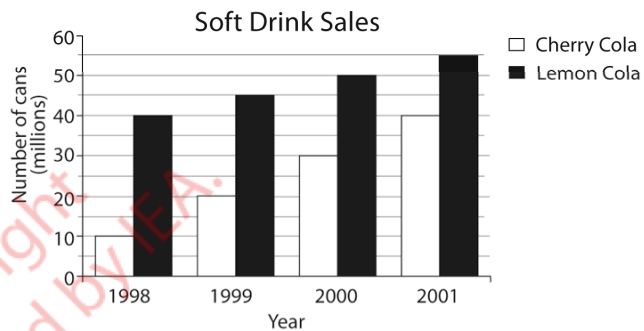
Maximum Points

1

Key

B

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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The graph shows the sales of two types of soft drink over 4 years. If the sales trends continue for the next 10 years, determine the year in which the sales of Cherry Cola will be the same as the sales of Lemon Cola.

- (A) 2003
- (B) 2004
- (C) 2005
- (D) 2006

Content Domain

Data and Chance

Topic Area

Data Interpretation

Cognitive Domain

Reasoning

Maximum Points

1

Key

B

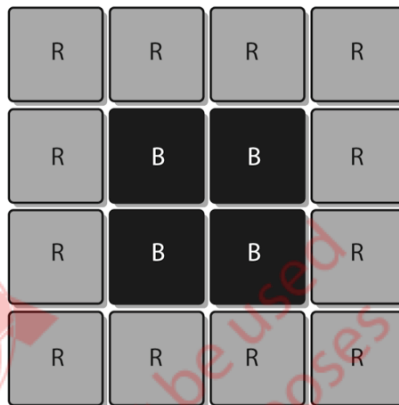
SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
 Publisher: TIMSS & PIRLS International Study Center, Lynch School of Education, Boston College.

Pat has red tiles and black tiles. Pat uses the tiles to make square shapes.

The 3×3 shape has 1 black tile and 8 red tiles.



The 4×4 shape has 4 black tiles and 12 red tiles.



The table below shows the number of tiles for the first three shapes Pat made. Pat continued making shapes using this pattern. Complete the table for the 6×6 and 7×7 shapes.

Shape	Number of Black Tiles	Number of Red Tiles	Total Number of Tiles
3×3	1	8	9
4×4	4	12	16
5×5	9	16	25
6×6	16		
7×7	25		

Questions for Red and Black Tiles continue. ➡

Content Domain

Algebra

Topic Area

Patterns

Cognitive Domain

Reasoning

Maximum Points

2

Key

See scoring guide

Use the patterns in the previous table to answer the following questions.

- A. Pat made a shape with a **total** of 64 tiles, how many were black and how many were red?

Answer: _____ black tiles _____ red tiles

- B. Pat made a shape that used 49 **black** tiles.
How many **red** tiles did Pat use in that shape?

Answer: _____ red tiles

- C. Next, Pat made a shape using 44 of the **red** tiles. How many black tiles would Pat need to complete the black part of the shape?

Answer: _____ black tiles

Content Domain

Algebra

Topic Area

Patterns

Cognitive Domain

Reasoning

Maximum Points

2

Key

See scoring guide

M032760

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
Publisher: TIMSS & PIRLS International Study Center, Lynch School of Education, Boston College.

Pat wanted to add a line to the table showing how to find the number of tiles needed to make a square of any size. Use the patterns in the table on the opposite page to help you complete the line for shape $n \times n$ in the table below.

Shape	Number of Black Tiles	Number of Red Tiles	Total Number of Tiles
$n \times n$	$(n - 2)^2$		

End of Red and Black Tiles section.

Content Domain

Algebra

Topic Area

Algebraic Expressions

Cognitive Domain

Reasoning

Maximum Points

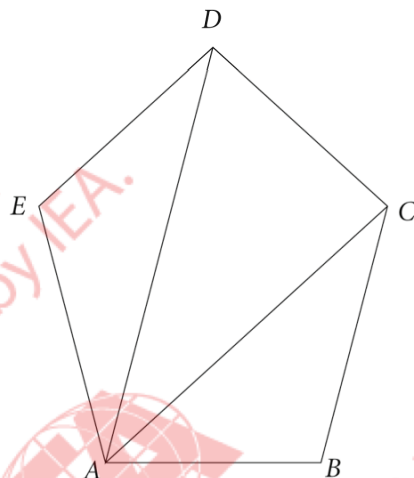
2

Key

See scoring guide

M032761

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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What is the sum of all the interior angles of pentagon $ABCDE$?
Show your work.

Answer: _____

Content Domain

Geometry

Topic Area

Geometric Shapes

Cognitive Domain

Reasoning

Maximum Points

2

Key

See scoring guide

M032692

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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Which of these shows how 36 can be expressed as a product of prime factors?

- (A) 6×6
- (B) 4×9
- (C) $4 \times 3 \times 3$
- (D) $2 \times 2 \times 3 \times 3$

M032626

Content Domain

Number

Topic Area

Whole Numbers

Cognitive Domain

Knowing

Maximum Points

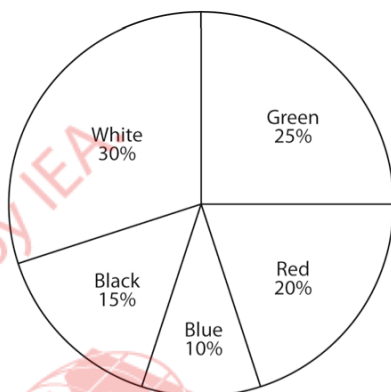
1

Key

D

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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Color of Caps



The pie chart shows the percentage of caps for sale at a sporting goods store. If there are 200 caps, what is the total number of caps that are either white or green?

- (A) 55
- (B) 100
- (C) 110
- (D) 145

Content Domain

Number

Topic Area

Ratio, Proportion and Percent

Cognitive Domain

Applying

Maximum Points

1

Key

C

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
Publisher: TIMSS & PIRLS International Study Center, Lynch School of Education, Boston College.

If t is a number between 6 and 9, then $t + 5$ is between what two numbers?

- (A) 1 and 4
- (B) 10 and 13
- (C) 11 and 14
- (D) 30 and 45

M032673

Content Domain

Algebra

Topic Area

Algebraic Expressions

Cognitive Domain

Knowing

Maximum Points

1

Key

C

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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Which number is equal to $\frac{3}{5}$?

- (A) 0.8
- (B) 0.6
- (C) 0.53
- (D) 0.35

M052216

Content Domain

Number

Topic Area

Fractions and Decimals

Cognitive Domain

Knowing

Maximum Points

1

Key

B

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$$42.65 + 5.748 =$$

Answer: _____

M052231

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Content Domain

Number

Topic Area

Fractions and Decimals

Cognitive Domain

Knowing

Maximum Points

1

Key

See scoring guide

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
Publisher: TIMSS & PIRLS International Study Center, Lynch School of Education, Boston College.

Kim is packing eggs into boxes.

Each box holds 6 eggs.

She has 94 eggs.

What is the smallest number of boxes she needs to pack all the eggs?

Answer: _____ boxes

Content Domain

Number

Topic Area

Whole Numbers

Cognitive Domain

Applying

Maximum Points

1

Key

See scoring guide

M052061



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Which shows a correct method for finding $\frac{1}{3} - \frac{1}{4}$?

(A) $\frac{1-1}{4-3}$

(B) $\frac{1}{4-3}$

(C) $\frac{3-4}{3 \times 4}$

(D) $\frac{4-3}{3 \times 4}$

Content Domain

Number

Topic Area

Fractions and Decimals

Cognitive Domain

Applying

Maximum Points

1

Key

D

M052228

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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Which of these number sentences is true?

(A) $\frac{3}{10}$ of 50 = 50% of 3

(B) 3% of 50 = 6% of 100

(C) $50 \div 30 = 30 \div 50$

(D) $\frac{3}{10} \times 50 = \frac{5}{10} \times 30$

Content Domain

Number

Topic Area

Fractions and Decimals

Cognitive Domain

Knowing

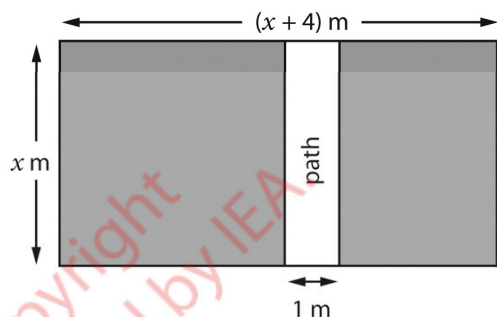
Maximum Points

1

Key

D

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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This is a diagram of a rectangular garden.

The white area is a rectangular path that is 1 meter wide.

Which expression shows the area of the shaded portion of the garden in m^2 ?

- (A) $x^2 + 3x$
- (B) $x^2 + 4x$
- (C) $x^2 + 4x - 1$
- (D) $x^2 + 3x - 1$

Content Domain

Algebra

Topic Area

Algebraic Expressions

Cognitive Domain

Applying

Maximum Points

1

Key

A

$$y = \frac{a+b}{c}$$

$a = 8$, $b = 6$, and $c = 2$

What is the value of y ?

- (A) 7
(B) 10
(C) 11
(D) 14

Content Domain

Algebra

Topic Area

Equations/ Formulas and Functions

Cognitive Domain

Knowing

Maximum Points

1

Key

A

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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A piece of wood was 40 cm long.

It was cut into 3 pieces.

The lengths in cm are

$$2x - 5$$

$$x + 7$$

$$x + 6$$

What is the length of the longest piece?

Answer: _____ cm

Show your work. If you use a calculator, you still must describe all the steps you used to obtain your answer.

Content Domain

Algebra

Topic Area

Equations/ Formulas and Functions

Cognitive Domain

Applying

Maximum Points

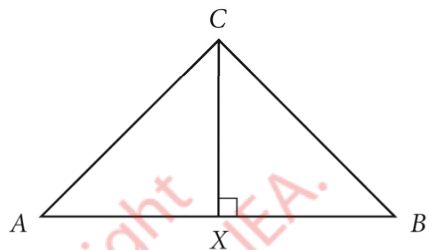
2

Key

See scoring guide

M052002

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In this triangle:

$$AC = BC$$

AB is twice as long as CX .

What is the size of angle B ?

Answer: _____ °

Content Domain

Geometry

Topic Area

Geometric Shapes

Cognitive Domain

Reasoning

Maximum Points

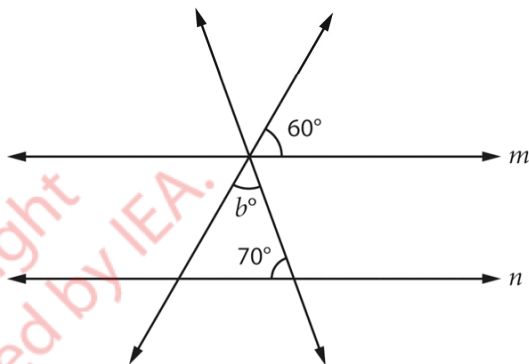
1

Key

See scoring guide

M052362

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Lines m and n are parallel.

What is the value of b ?

Answer: _____

Content Domain

Geometry

Topic Area

Geometric Shapes

Cognitive Domain

Reasoning

Maximum Points

1

Key

See scoring guide

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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The perimeter of a square is 36 cm.

What is the area of this square?

- (A) 81 cm^2
- (B) 36 cm^2
- (C) 24 cm^2
- (D) 18 cm^2

Content Domain

Geometry

Topic Area

Geometric Measurement

Cognitive Domain

Applying

Maximum Points

1

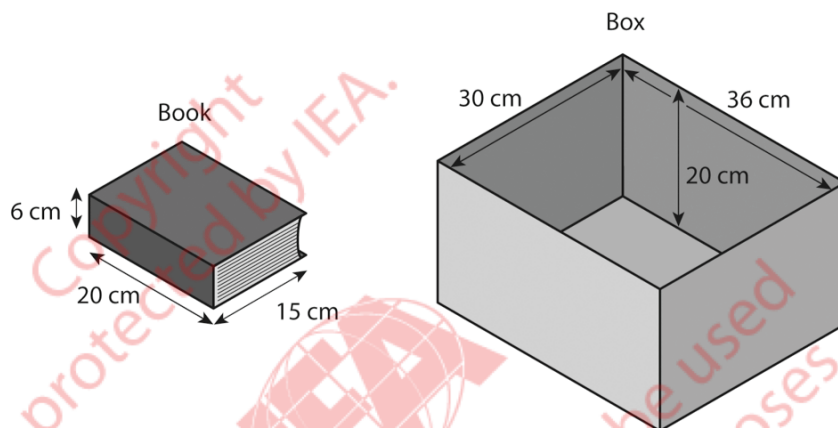
Key

A

M052084

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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Ryan is packing books into a rectangular box.
All the books are the same size.



What is the largest number of books that will fit inside the box?

Answer: _____

Content Domain

Geometry

Topic Area

Geometric Measurement

Cognitive Domain

Reasoning

Maximum Points

1

Key

See scoring guide

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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There are 10 marbles in a bag: 5 red, and 5 blue.

Sue draws a marble from the bag at random. The marble is red.

She puts the marble back into the bag.

What is the probability that the next marble she draws at random is red?

- (A) $\frac{1}{2}$
- (B) $\frac{4}{10}$
- (C) $\frac{1}{5}$
- (D) $\frac{1}{10}$

**Content Domain**

Data and Chance

Topic Area

Chance

Cognitive Domain

Reasoning

Maximum Points

1

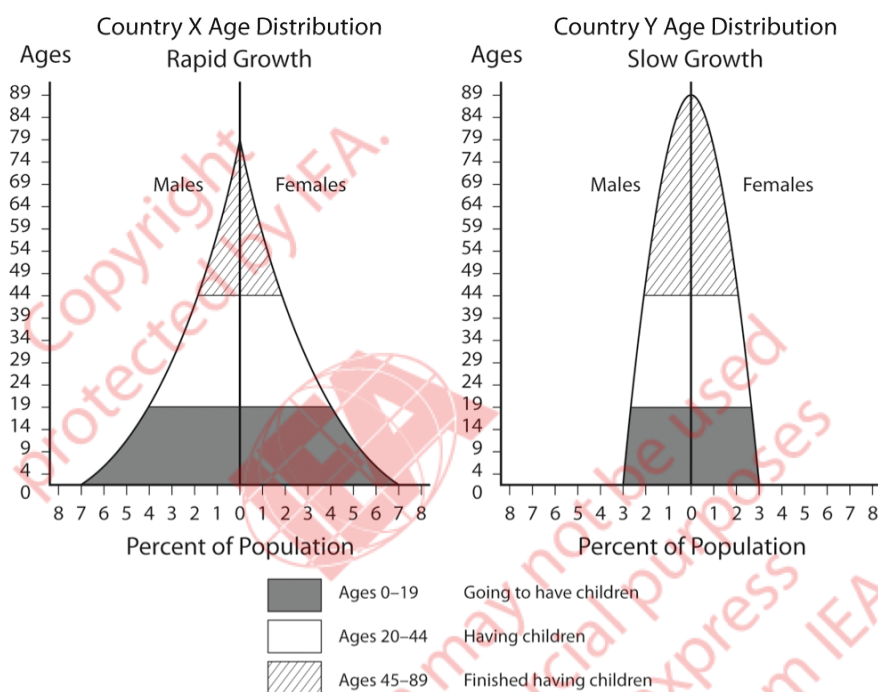
Key

A

M052429

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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Comparison of Age Structure Between Country X and Country Y



The graphs for Country X and Country Y show the age structure of each country's population. The population is divided into three age groups from youngest to oldest. The graphs enable predictions about population growth.

- A. Why could the age structure of Country X lead to more rapid population growth than the age structure of Country Y?
- B. Why could Country Y expect to have a bigger problem taking care of its elderly population than Country X?

Content Domain

Data and Chance

Topic Area

Data Interpretation

Cognitive Domain

Reasoning

Maximum Points

1

Key

See scoring guide

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
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Which fraction is equivalent to 0.125?

- (A) $\frac{125}{100}$
- (B) $\frac{125}{1,000}$
- (C) $\frac{125}{10,000}$
- (D) $\frac{125}{100,000}$

Content Domain

Number

Topic Area

Fractions and Decimals

Cognitive Domain

Knowing

Maximum Points

1

Key

B

M042032

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
Publisher: TIMSS & PIRLS International Study Center, Lynch School of Education, Boston College.

The fractions $\frac{4}{14}$ and $\frac{\square}{21}$ are equivalent.

What is the value of \square ?

- (A) 6
- (B) 7
- (C) 11
- (D) 14

Content Domain

Number

Topic Area

Fractions and Decimals

Cognitive Domain

Applying

Maximum Points

1

Key

A

SOURCE: TIMSS 2011 Assessment. Copyright © 2013 International Association for the Evaluation of Educational Achievement (IEA).
Publisher: TIMSS & PIRLS International Study Center, Lynch School of Education, Boston College.

Here is a pattern:

$$3 - 3 = 0$$

$$3 - 2 = 1$$

$$3 - 1 = 2$$

$$3 - 0 = 3$$

What will the next line in the pattern be?

Answer:

**Content Domain**

Number

Topic Area

Integers

Cognitive Domain

Reasoning

Maximum Points

1

Key

See scoring guide

M042186

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Peter, James, and Andrew each had 20 tries at throwing balls into a basket.
Complete the missing boxes below.

Name	Number of Successful Shots	Percentage of Successful Shots
Peter	10 out of 20	50 %
James	15 out of 20	<input type="text"/>
Andrew	<input type="text"/> out of 20	80%

Content Domain

Number

Topic Area

Ratio, Proportion and Percent

Cognitive Domain

Knowing

Maximum Points

2

Key

See scoring guide

M042059

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